

# The stellar initial mass function of early-type galaxies from low to high stellar velocity dispersion: homogeneous analysis of ATLAS<sup>3D</sup> and Sloan Lens ACS galaxies

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#### **ABSTRACT**

We present an investigation about the shape of the initial mass function (IMF) of early-type galaxies (ETGs), based on a joint lensing and dynamical analysis, and on stellar population synthesis models, for a sample of 55 lens ETGs identified by the Sloan Lens Advanced Camera for Surveys (SLACS). We construct axisymmetric dynamical models based on the Jeans equations which allow for orbital anisotropy and include a dark matter halo. The models reproduce in detail the observed *Hubble Space Telescope* photometry and are constrained by the total projected mass within the Einstein radius and the stellar velocity dispersion ( $\sigma$ ) within the Sloan Digital Sky Survey fibres. Comparing the dynamically-derived stellar mass-to-light ratios  $(M_*/L)_{\rm dyn}$ , obtained for an assumed halo slope  $\rho_{\rm h} \propto r^{-1}$ , to the stellar population ones  $(M_*/L)_{Salp}$ , derived from full-spectrum fitting and assuming a Salpeter IMF, we infer the mass normalization of the IMF. Our results confirm the previous analysis by the SLACS team that the mass normalization of the IMF of high- $\sigma$  galaxies is consistent on average with a Salpeter slope. Our study allows for a fully consistent study of the trend between IMF and  $\sigma$  for both the SLACS and atlas<sup>3D</sup> samples, which explore quite different  $\sigma$  ranges. The two samples are highly complementary, the first being essentially  $\sigma$  selected, and the latter volumelimited and nearly mass selected. We find that the two samples merge smoothly into a single trend of the form  $\log \alpha = (0.38 \pm 0.04) \times \log (\sigma_e/200 \,\mathrm{km \, s^{-1}}) + (-0.06 \pm 0.01)$ , where  $\alpha = (M_*/L)_{\rm dyn}/(M_*/L)_{\rm Salp}$  and  $\sigma_{\rm e}$  is the luminosity averaged  $\sigma$  within one effective radius Re. This is consistent with a systematic variation of the IMF normalization from Kroupa to Salpeter in the interval  $\sigma_e \approx 90-270 \, \mathrm{km \, s^{-1}}$ .

**Key words:** galaxies: elliptical and lenticular, cD – galaxies: evolution – galaxies: formation – galaxies: kinematics and dynamics – galaxies: structure.

## 1 INTRODUCTION

The stellar initial mass function (IMF) describes the mass distribution of the stellar population originated in a single star formation burst, at the time of birth. It gives us information about the relative importance of low- and high-mass stars, hence its form directly affects the amount of stellar ejecta and their chemical composition, the mass distribution of stellar remnants, and the stellar mass-to-light ratio of the population. The study of the shape of the IMF also gives us direct insights into the physics of star formation, and it is crucial for the estimate of galaxy stellar masses starting from

the observed luminosity. Thus, the knowledge of the IMF is fundamental in many fields of astrophysics that study the formation and evolution of stellar systems. Several direct measurements of star counts of resolved stellar populations in the solar neighbourhood have shown that the IMF can be parametrized by a power-law mass distribution  $dN/dM \propto M^{-s}$ , characterized by a Salpeter (1955) slope  $s \simeq 2.35$  for  $M \gtrsim 0.5$  M $_{\odot}$ , and by a change towards flatter slopes for  $M \lesssim 0.5$  M $_{\odot}$  (Kroupa 2001; Chabrier 2003). This holds in different environments throughout the Milky Way (Kroupa 2002; Bastian, Covey & Meyer 2010), but whether this is true for all galaxies is still ongoing debate. Stellar counts down to very low stellar masses (i.e. in the mass range of major uncertainty given the intrinsic difficulty of measurements) is not feasible in distant external galaxies, so that, in order to study the extragalactic IMF, people use alternative

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methods based, for example, on ionized gas emission, redshift evolution of the tilt and normalization of the Fundamental Plane, strength of IMF-sensitive spectral features, gas kinematics, gravitational lensing and stellar dynamics (see Cappellari et al. 2013b for a more detailed review). Among these indirect methods, it is widely used to constrain the IMF shape by estimating galaxy stellar masses from dynamical models and comparing them with the predictions of stellar population synthesis models, that rely on an assumed IMF shape. Note that this method does not directly measure the shape of the IMF, but its overall mass normalization: each IMF shape results in a different  $M_*/L$ , that is converted in a different stellar mass, once the luminosity is measured. In the last decade, a number of works based on this method have agreed that spiral galaxies are inconsistent with a Salpeter normalization over the whole mass range, and that they need a lighter overall normalization similar to Kroupa or Chabrier, like the Milky Way (Bell & de Jong 2001; Kassin et al. 2006; Bershady et al. 2011; Brewer et al. 2012). The same result also appears to be valid for at least some early-type galaxies (ETGs; Cappellari et al. 2006; Ferreras, Saha & Burles 2008; Dutton et al. 2011; Thomas et al. 2011; Brewer et al. 2014; Peacock et al. 2014), thus showing no evidence of a departure from a universal stellar IMF.

In contrast, however, there are numerous works carried out on ETG samples that point out evidences of a dynamical mass excess over the predictions of stellar population models with fixed IMF. This excess increases with galaxy mass and it can be explained either (i) by an IMF normalization that increases from a Kroupa/Chabrier one at low masses, up to a Salpeter normalization for the more massive galaxies, implying a systematic variation of the IMF (e.g. Renzini & Ciotti 1993), or (ii) by an increase of the dark matter (DM) fraction as function of galaxy mass due to a nonuniversal DM halo profile (Padmanabhan et al. 2004; Cappellari et al. 2006; Grillo et al. 2009; Thomas et al. 2009; Tortora et al. 2009; Auger et al. 2010; Graves & Faber 2010; Schulz, Mandelbaum & Padmanabhan 2010; Treu et al. 2010, hereafter T10; Barnabè et al. 2011; Dutton, Mendel & Simard 2012; Tortora, Romanowsky & Napolitano 2013). This method, based on the comparison between galaxy stellar masses computed from dynamical and stellar population synthesis models, is indeed subject to degeneracies in the dynamical modelling, which are related to the assumptions for the luminous and DM density profiles, and for the velocity dispersion anisotropy. However, the degeneracies can be reduced by additional constraints derived, for example, from gravitational lensing analysis or integral-field spectroscopy observations.

An example is given by the results of the Sloan Lens Advanced Camera for Surveys (SLACS) group: T10 analysed 56 lens ETGs belonging to the SLACS sample by building dynamical models tuned to reproduce the Sloan Digital Sky Survey (SDSS) measured velocity dispersion  $\sigma_*$  and the total projected mass within the Einstein radius. They adopted two-component spherical isotropic dynamical models with self-similar Hernquist (1990) profiles to describe the stellar density, and an NFW (Navarro, Frenk & White 1997) DM density distribution with fixed slope and scale radius. T10 found that bottom-heavy IMFs such as Salpeter are strongly preferred over light-weight IMFs such as Kroupa/Chabrier for the most massive ETGs, assuming standard NFW DM density profiles. This result was then strengthened by Auger et al. (2010) who included adiabatic contraction and weak-lensing constraints in the modelling, and found that only Salpeter-like IMF are consistent with the observed properties of their ETG sample. Note this is an effectively velocity dispersion selected sample, so that it is composed of high- $\sigma$ galaxies (see Section 2 and references therein).

Another remarkable example is the work of Cappellari et al. (2012, 2013a,b) on the volume-limited, nearly mass selected atlas ample of 260 ETGs. They constructed detailed axisymmetric dynamical models, which allow for orbital anisotropy and reproduce in detail both the galaxy images and the high-quality integral-field stellar kinematics out to about one effective radius  $R_{\rm e}$ . Given the tighter constraints with respect to previous analogous studies, their models were well suited to explore different DM density profiles, and they find that a non-universal IMF is always required under all halo assumptions, due to the low DM mass contribution within  $R_{\rm e}$ . Their study, based on an unprecedented large sample of ETGs spanning a wide range in galaxy mass, found a systematic trend in IMF normalization varying from Kroupa/Chabrier up to Salpeter or heavier for increasing velocity dispersion.

Finally other works, based on IMF-sensitive spectral features, that are completely independent of dynamical modelling assumptions, find a steepening IMF with increasing velocity dispersion and [Mg/Fe], with massive ETGs requiring bottom-heavy, dwarf-rich IMF (van Dokkum & Conroy 2010, 2011; Conroy & van Dokkum 2012; Spiniello et al. 2012, 2014; Ferreras et al. 2013). Thus, there seems to be a systematic dependence of the IMF on galaxy properties, indicating that high-mass ETGs prefer on average a Salpeter normalization, while low-mass galaxies are consistent with a lighter normalization, similar to Kroupa or Chabrier. However, quantitative consistency between the dynamical and spectral synthesis approach has not been achieved yet (e.g. Smith 2014; McDermid et al. 2014).

In this work, we revisit the analysis of T10 in order to investigate the effects of a more detailed modelling of the stellar component. T10 spherical models indeed provide only a crude approximation to the observed galaxy surface brightness, which shows evidence for discs and it is known to vary systematically with galaxy mass (Caon, Capaccioli & D'Onofrio 1993). To address this potential bias, here we construct models which allow for axisymmetry and can reproduce the observed galaxy surface brightness in detail, in an essentially non-parametric way. Moreover, differently from T10, our stellar population synthesis models are built via full spectrum fitting of SDSS spectra, and not by means of multicolour photometry. An approach closely related to the one illustrated in this work, was employed also by Barnabè et al. (2013) in their analysis of two SLACS ETGs, where they also exploited X-Shooter spatially resolved kinematic data in order to put constraints on these systems' IMFs.

Finally, our analysis is similar to that performed by Cappellari et al. (2013a); therefore, this allows us also to combine the SLACS and the atlas<sup>3D</sup> samples, obtaining a larger and homogeneously analysed sample of ETGs. Remarkably, due to their selection criteria the two samples are complementary, so that the combined sample is fairly representative of ETGs, extending from low to very high velocity dispersions (or stellar masses). Another attempt to compare similar previous works was made by Dutton et al. (2013b), even though it is not as homogeneous as this.

We proceed as follows. In Section 2, we briefly summarize the sample and data, while in Section 3, we describe our dynamical and stellar population synthesis models. The main results are presented in Section 4, and Section 5 summarizes the conclusions. All magnitudes are in the AB photometric system, and a standard concordance cosmology is assumed, i.e. h=0.7,  $\Omega_{\rm m}=0.3$  and  $\Omega_{\Lambda}=0.7$ .

# 2 SAMPLE AND DATA

The subsample of galaxies analysed in this work is extracted from the SLACS sample studied in T10. The SLACS sample is

composed of massive ETGs, that were spectroscopically selected from the SDSS data base for being gravitational lenses (Bolton et al. 2006). In particular, the SLACS sample consists of galaxies with very high  $\sigma$  for two main reasons: (i) the lensing cross-section scales approximately with  $\sigma^4$ , and (ii) the SDSS is a flux-limited sample, so that high-luminosity, and therefore high- $\sigma$ , galaxies are overrepresented because they are visible over a larger volume (Hyde & Bernardi 2009). Thus, the SLACS sample is effectively  $\sigma$ -selected (Auger et al. 2010; Ruff et al. 2011). Several studies have shown that the SLACS sample is indistinguishable from a  $\sigma$ -selected sample of non-lens ETGs (Bolton et al. 2006; Treu et al. 2006, 2009).

We selected our SLACS subsample by requiring the availability of *Hubble Space Telescope (HST)* photometry in the *I* band, since it is expected to better trace the luminous mass, being less affected by the presence of dust. In this way, we obtained a subsample of 55 galaxies that span a redshift range of  $0.06 \lesssim z \lesssim 0.36$ . Our data consist of *HST/ACS/F814W* images (Auger et al. 2009), and SDSS optical spectra taken from data release ten (DR10; Ahn et al. 2014). SDSS spectra cover the wavelength range 3800–9200 Å, with a spectral resolution of  $\sim$ 2.76 Å FWHM, which corresponds to an intrinsic dispersion  $\sigma_{\rm int} \sim$ 85 km s<sup>-1</sup> at 3800 Å and  $\sigma_{\rm int} \sim$ 50 km s<sup>-1</sup> at 9000 Å.

# 3 METHODS

In order to study the mass normalization of the IMF for our sample of 55 ETGs, we compare the stellar mass-to-light ratios  $M_*/L$  determined from two different and independent diagnostics of galaxy stellar mass. The first method relies on gravitational lensing and stellar kinematics, it involves the construction of dynamical models, and so it is sensitive to galaxy mass structure and stellar dynamics assumptions (Section 3.1). Here, we try to reduce the unavoidable degeneracies generating from the assumption of a particular stellar profile, by using a parametrization which allows for a large number of free parameters. This approach is able to reproduce the galaxy surface brightness images in detail, adding new parameters until the difference between the model and the image becomes negligible. The second approach is instead based on stellar population synthesis models, it assumes an IMF, and returns an estimate of  $M_*/L$ by means of spectral fitting; the reliability of this method depends mostly on the goodness of the stellar templates (Section 3.2).

# 3.1 The dynamical modelling

#### 3.1.1 The mass structure

The mass structure of our galaxy models consists of three components: an axisymmetric stellar distribution, a spherical DM halo, and a central supermassive black hole (BH).

The stellar component is accurately modelled with the aid of *I*-band *HST* images on which we performed a multi-Gaussian expansion (MGE) axisymmetric parametrization (Emsellem et al. 1994; see also Bendinelli 1991; Bendinelli, Ciotti & Parmeggiani 1993) that fits the galaxy surface brightness distribution. In particular, we used the MGE\_FIT\_SECTORS software package of Cappellari (2002),<sup>1</sup> where the MGE formalism and the fitting algorithm are fully described. Given the nature of our sample, the galaxy images are characterized by the presence of several gravitational arches or rings that

we properly mask in order to obtain a better fit. We impose the surface brightness profile of the MGE model to decrease as  $R^{-4}$  at large radii, so as to limit the inclusion of spurious light from nearby galaxies. All the model Gaussians are convolved with a Gaussian point spread function (PSF) with a dispersion of 0.04 arcsec, as befitting for ACS. We also use some prescriptions for the Gaussians' axial ratio: in the limits of obtaining a good fit of the surface brightness, we force (1) the flattest Gaussian to have the highest axial ratio, and (2) the Gaussians' axial ratio range to be the smallest possible. In this way, we both avoid an artificial restriction of the range of the possible inclination angles for which the model can be deprojected (see Cappellari 2002, section 2.2.2), and we 'regularize' the model, preventing significant variations of the axial ratio, as physically plausible. These assumptions are needed because the deprojection, to obtain the intrinsic stellar luminosity density from the observed surface brightness, is mathematically non-unique (Rybicki 1987; Gerhard & Binney 1996). Moreover, some of the galaxies have been observed only once so that we remove the presence of cosmic rays using the LA\_COSMIC software of van Dokkum (2001).<sup>2</sup> The model flux is corrected for foreground galactic extinction following Schlafly & Finkbeiner (2011), as given by the NASA/IPAC Extragalactic Database, and the apparent *I*-band magnitude  $m_I$  is computed, assuming  $M_{\odot I} = 4.57^{3}$ . Then, by means of SDSS spectra, we perform a k-correction following Hogg et al. (2002), and we transform all observed magnitudes to consistent V- and r-band rest-frame magnitudes,  $M_V$  and  $M_r$ , respectively, assuming the redshift values reported in Table 1. This correction was necessary due to the non-negligible redshift range spanned by the galaxies, and the choice of the photometric bands is motivated by the possibility to compare our results with the SLACS and atlas3D ones, that have been obtained in these bands. Then, assuming  $M_{\odot r} = 4.64$ (Blanton & Roweis 2007), we normalized the model Gaussians in units of  $L_{\bigcirc r}$  pc<sup>-2</sup>, so that now the MGE model has the right units and format to be used for the dynamical modelling (see Section 3.1.2). The MGE models for all the 55 galaxies are shown in Fig. 1, Table 1 reports their magnitudes, and all their parameters are listed in Appendix A. As a sanity check, we compared our  $m_I$  with the ones reported by Bolton et al. (2008): their magnitudes were calculated, starting from the same data, by fitting two-dimensional ellipsoidal de Vaucouleurs (1948) luminosity profiles, and are the result of the full (not truncated) analytic integral of the best-fitting de Vaucouleurs model. We find that the two sets of magnitudes agree with an rms scatter of 0.08 mag, but our  $m_I$  are systematically higher by 0.18 mag, implying fluxes underestimated by 18 per cent. This is likely due to the fact that SLACS magnitudes are extrapolated to infinite radii, while ours are limited to the observed photons. Finally, in Fig. 2 we compared our  $M_V$  with the magnitudes calculated by Auger et al. (2009) in the same band, and found they are consistent with an rms scatter of 0.07 mag, which implies an error of 5 per cent in the luminosity; we assume the same error also for  $M_r$ .

For what concerns the DM halo density distribution, we adopt the NFW (Navarro et al. 1997) profile for two main reasons. The first is imposed by the few observational constraints at our disposal (see Section 3.1.3), which prevent us from exploring a more flexible DM halo profile, since the addition of further parameters to the models would make the problem completely undetermined. Thus, our results are valid under the assumption that the NFW profile is reliable in providing fair estimates for the DM fraction. The second

<sup>&</sup>lt;sup>1</sup> Available at http://purl.org/cappellari/software.

<sup>&</sup>lt;sup>2</sup> Available at http://www.astro.yale.edu/dokkum/lacosmic/.

<sup>&</sup>lt;sup>3</sup> Taken from http://mips.as.arizona.edu/~cnaw/sun.html.

Table 1. Properties and jam models parameters of the 55 galaxy SLACS subsample.

Name	z	$\sigma_*$ (km s <sup>-1</sup> )	R <sub>EIN</sub> (kpc)	$\log M_{\rm EIN}$ $({ m M}_{\bigodot})$	$m_I$ (mag)	$M_V$ (mag)	$M_r$ (mag)	log R <sub>e</sub> <sup>maj</sup> (arcsec)	$\log R_{\rm e}$ (arcsec)
(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)	(10)
J0029-0055	0.2270	$229 \pm 18$	3.48	11.08	17.16	-22.67	-22.79	2.017	1.830
J0037-0942	0.1955	$279 \pm 14$	4.95	11.47	16.35	-23.09	-23.20	2.016	1.763
J0044+0113	0.1196	$266 \pm 13$	1.72	10.96	15.83	-22.38	-22.48	2.216	1.923
J0216-0813	0.3317	$333 \pm 23$	5.53	11.69	17.12	-23.70	-23.85	2.050	1.831
J0252+0039	0.2803	$164 \pm 12$	4.40	11.25	18.15	-22.24	-22.35	0.950	0.878
J0330-0020	0.3507	$212 \pm 21$	5.45	11.40	18.21	-22.75	-22.93	1.076	0.941
J0728+3835	0.2058	$214 \pm 11$	4.21	11.30	16.83	-22.73	-22.84	1.567	1.348
J0737+3216	0.3223	$338 \pm 17$	4.66	11.46	17.25	-23.49	-23.64	1.829	1.738
J0822+2652	0.2414	$259 \pm 15$	4.45	11.38	17.10	-22.89	-23.00	1.644	1.458
J0841 + 3824	0.1159	$225 \pm 11$	2.96	11.12	15.23	-22.86	-22.99	6.743	4.672
J0912+0029	0.1642	$326 \pm 16$	4.58	11.60	15.77	-23.22	-23.34	3.034	2.452
J0935-0003	0.3475	$396 \pm 35$	4.26	11.60	17.05	-23.89	-24.05	2.744	2.551
J0936+0913	0.1897	$243 \pm 12$	3.45	11.17	16.62	-22.74	-22.86	1.876	1.691
J0946+1006	0.2219	$263 \pm 21$	4.95	11.46	17.18	-22.58	-22.70	1.760	1.722
J0955+0101	0.1109	$192 \pm 13$	1.83	10.83	17.04	-20.89	-21.02	1.549	0.840
J0956+5100	0.2405	$334 \pm 17$	5.05	11.57	16.82	-23.18	-23.28	1.756	1.572
J0959+4416	0.2369	$244 \pm 19$	3.61	11.23	17.12	-22.82	-22.93	1.500	1.381
J0959+0410	0.1260	$197 \pm 13$	2.24	10.88	17.05	-21.24	-21.37	1.249	1.009
J1020+1122	0.2822	$282 \pm 18$	5.12	11.54	17.47	-22.94	-23.05	1.156	1.037
J1023+4230	0.1912	$242 \pm 15$	4.50	11.37	16.89	-22.48	-22.60	1.480	1.383
J1029+0420	0.1045	$210 \pm 11$	1.92	10.78	16.24	-21.66	-21.77	1.771	1.193
J1032+5322	0.1334	$296 \pm 15$	2.44	11.05	17.12	-21.36	-21.47	1.004	0.659
J1103+5322	0.1582	$196 \pm 12$	2.78	10.98	16.63	-22.27	-22.39	1.927	1.217
J1106+5228	0.0955	$262 \pm 13$	2.17	10.96	15.55	-22.12	-22.23	2.036	1.609
J1112+0826	0.2730	$320 \pm 20$	6.19	11.65	17.41	-22.90	-23.02	1.160	1.010
J1134+6027	0.1528	$239 \pm 12$	2.93	11.10	16.43	-22.38	-22.50	2.147	1.935
J1142+1001	0.2218	$221 \pm 22$	3.52	11.22	17.13	-22.65	-22.76	1.779	1.640
J1143-0144 J1153+4612	0.1060 0.1797	$269 \pm 13$ $226 \pm 15$	3.27 3.18	11.29 11.05	15.15 17.25	-22.72 $-21.97$	-22.84 $-22.08$	3.493 1.037	3.133 1.029
J1204+0358	0.1797	$267 \pm 17$	3.68	11.03	16.94	-21.97 $-22.04$	-22.08 $-22.16$	1.037	1.029
J1204+0338 J1205+4910	0.1044	$281 \pm 14$	4.27	11.40	16.81	-22.88	-23.00	1.977	1.706
J1203+4910 J1213+6708	0.2130	$291 \pm 14$ $292 \pm 15$	3.13	11.40	15.70	-22.56 $-22.57$	-23.60 $-22.69$	2.969	2.604
J1218+0830	0.1229	$219 \pm 13$	3.47	11.21	15.89	-22.61	-22.72	2.739	2.414
J1250+0523	0.2318	$252 \pm 14$	4.18	11.26	16.88	-23.01	-23.11	1.297	1.290
J1402+6321	0.2046	$267 \pm 17$	4.53	11.46	16.52	-23.02	-23.14	2.251	1.997
J1403+0006	0.1888	$213 \pm 17$	2.62	10.98	17.19	-22.14	-22.26	1.131	1.041
J1416+5136	0.2987	$240 \pm 25$	6.08	11.56	17.71	-22.85	-22.97	1.227	1.082
J1420+6019	0.0629	$205 \pm 10$	1.26	10.59	15.19	-21.54	-21.65	2.048	1.575
J1430+4105	0.2850	$322 \pm 32$	6.53	11.73	16.96	-23.49	-23.58	1.728	1.668
J1432+6317	0.1230	$199 \pm 10$	2.78	11.05	15.44	-22.80	-22.93	3.751	3.724
J1436-0000	0.2852	$224 \pm 17$	4.80	11.36	17.41	-23.03	-23.13	1.776	1.587
J1443+0304	0.1338	$209 \pm 11$	1.93	10.78	17.02	-21.45	-21.57	1.230	0.984
J1451-0239	0.1254	$223 \pm 14$	2.33	10.92	16.08	-22.21	-22.33	2.167	2.010
J1525+3327	0.3583	$264 \pm 26$	6.55	11.68	17.39	-23.63	-23.79	2.180	1.773
J1531-0105	0.1596	$279 \pm 14$	4.71	11.43	15.95	-22.92	-23.04	2.573	2.201
J1538+5817	0.1428	$189 \pm 12$	2.50	10.95	16.78	-21.87	-21.98	1.384	1.270
J1621+3931	0.2449	$236 \pm 20$	4.97	11.47	16.95	-23.09	-23.22	1.908	1.698
J1627-0053	0.2076	$290 \pm 15$	4.18	11.36	16.92	-22.66	-22.78	1.660	1.514
J1630+4520	0.2479	$276\pm16$	6.91	11.69	17.00	-23.06	-23.18	1.537	1.394
J1636+4707	0.2282	$231 \pm 15$	3.96	11.25	17.17	-22.67	-22.78	1.402	1.272
J2238-0754	0.1371	$198 \pm 11$	3.08	11.11	16.33	-22.18	-22.30	1.963	1.748
J2300+0022	0.2285	$279 \pm 17$	4.51	11.47	17.22	-22.61	-22.73	1.410	1.298
J2303+1422	0.1553	$255\pm16$	4.35	11.42	16.07	-22.69	-22.83	2.591	2.108
J2321-0939	0.0819	$249 \pm 12$	2.47	11.08	14.82	-22.44	-22.56	3.316	2.963
J2341+0000	0.1860	$207 \pm 13$	4.50	11.35	16.48	-22.81	-22.94	2.661	2.078

Notes: (1) Galaxy name. (2) and (3) Galaxy redshift and SDSS-measured stellar velocity dispersion within the spectroscopic aperture of diameter 3 arcsec, both taken from T10, their table 1. (4) and (5) Einstein radius and total projected mass within a cylinder of radius equal to  $R_{\rm EIN}$ , taken from Auger et al. (2009), their table 4. (6) *I*-band apparent magnitude (*F*814*W*) derived from the MGE model (1 $\sigma$  random error of 0.06 mag). (7) and (8) *V*- and *r*-band absolute magnitudes (1 $\sigma$  random error of 0.05 mag). (9) Major axis of the isophote containing half of the analytic total light of the MGE models (1 $\sigma$  error of 10 per cent or 0.041 dex). (10) Circularized effective radius  $R_e = \sqrt{A_e/\pi}$  where  $A_e$  is the area of the effective isophote containing half of the analytic total light of the MGE models (same error as  $R_e^{\rm maj}$ ).

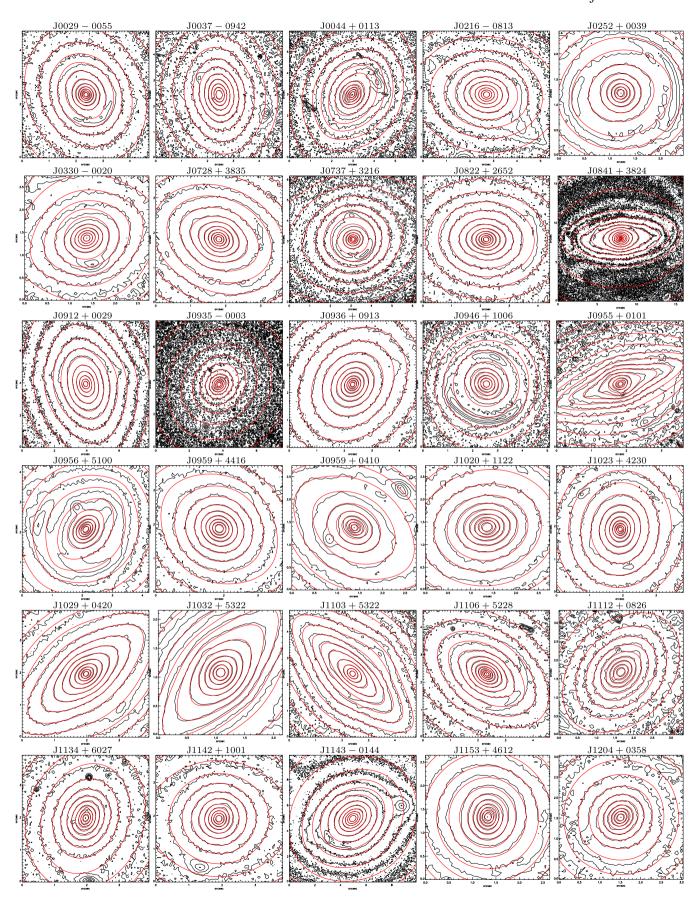


Figure 1. Contour maps of the central regions ( $\sim$ 0.5  $R_{\rm e}$ ) of the Wide Field Channel F814W (*I*-band) images of the 55 galaxies (black). The contours of the MGE surface brightness, convolved with the proper PSF, are superimposed in red.

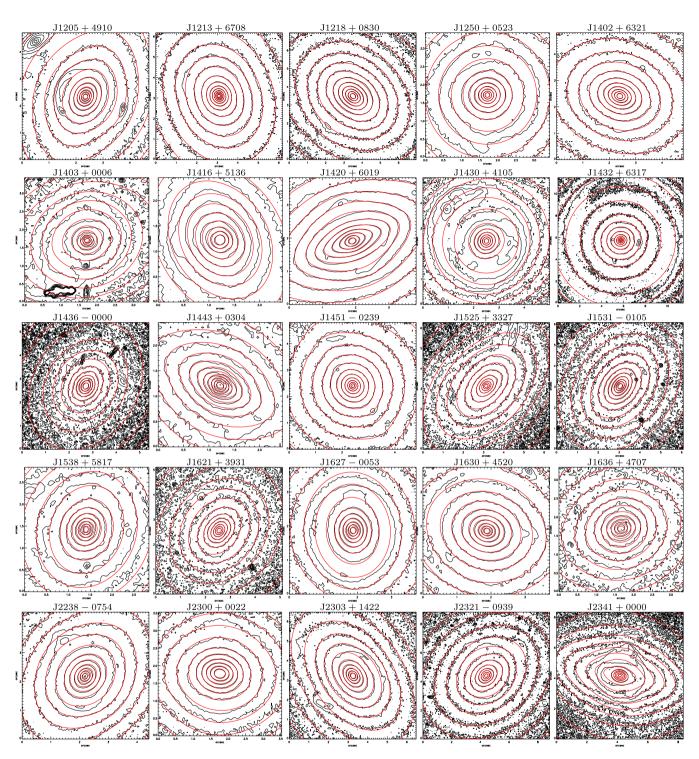


Figure 1 - continued

reason is that one of the motivations of this study is to investigate the possible bias introduced by T10 with the use of spherical isotropic Hernquist models to describe the stellar components of the SLACS sample, that is apparently composed of non-spherical galaxies (see Fig. 1). Thus, in order to disentangle the effects produced by this approximation, we make use of the same DM density profile adopted by T10, that is the untruncated NFW profile

$$\rho_{\rm h}(r) = \frac{\rho_{\rm crit} \delta_{\rm c} r_{\rm h}}{r \left(1 + r/r_{\rm h}\right)^2},\tag{1}$$

with fixed  $r_h = 30$  kpc. We then perform a one-dimensional MGE fit to equation (1) in order to recover the DM surface density in units of  $M_{\odot}$  pc<sup>-2</sup>, and add the DM halo to the dynamical modelling (Section 3.1.2).

Finally, we apply a similar procedure for the BH, parametrizing it with a single Gaussian with a dispersion of 0.01 arcsec. The BH mass is chosen adopting the  $M_{\rm BH}$ – $\sigma_{\rm e}$  relation of Gültekin et al. (2009) for elliptical galaxies, where, for each galaxy,  $\sigma_{\rm e}$  (i.e. the luminosity averaged stellar velocity dispersion within  $R_{\rm e}$ ) is

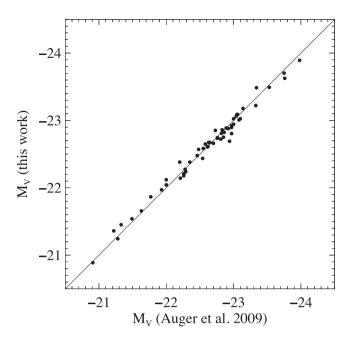


Figure 2. V-band absolute magnitudes for the SLACS sample, computed here and in Auger et al. (2009).

computed starting from  $\sigma_*$  (the SDSS-measured velocity dispersion, luminosity-averaged within a circular aperture of radius 1.5 arcsec) and using the conversion formula in equation 1 of Cappellari et al. (2006), thus accounting for aperture correction.

## 3.1.2 The stellar kinematics

The model velocity fields are computed using the Jeans anisotropic MGE (jam) modelling method of Cappellari (2008), which can be applied to an axisymmetric stellar distribution, described by a three-integral distribution function. This method assumes a velocity ellipsoid aligned with the cylindrical coordinates  $(R, z, \varphi)$ , and a constant vertical anisotropy parametrized by  $\beta_z = 1 - \sigma_z^2/\sigma_R^2$ . For our models we fix  $\beta_z = 0.2$ , which has been found to be representative of local ETGs (Cappellari et al. 2007). However, relaxing this assumption, and considering isotropic models ( $\beta_z = 0$ ) as done in T10, negligibly affects our results. Moreover, for simplicity we assume a spatially constant  $M_*/L$ , even if recent studies found evidences for an IMF dependence on galactocentric distance (e.g. Martín-Navarro et al. 2014; Pastorello et al. 2014). These evidences do not make our results invalid, since this assumption simply implies that our measured  $M_*/L$  represents a mean value in the observed region (which typically has size  $r \lesssim R_e$ ), as already done by Cappellari et al. (2013a). This does not exclude, for example, that the IMF might be universal in the outer disc components and vary only within bulges or spheroids (see e.g. Dutton et al. 2013a).

The main ingredients of the dynamical modelling are the galaxy surface brightness in units of  $L_{\odot}$  pc<sup>-2</sup>, and the galaxy surface density of the total mass distribution in units of  $M_{\odot}$  pc<sup>-2</sup>. This last is the sum of the three components (stars, DM and BH) obtained as described in Section 3.1.1, where the stellar one is multiplied by a stellar mass-to-light ratio  $(M_*/L)_{\rm dyn}$  that is the quantity we want to retrieve (as will be explained in Section 3.1.3). Then the only free parameters left are  $\beta_z$  and the inclination angle i, whose values have to be provided or assumed. Indeed, once the MGE parametrization of the surface brightness profile is obtained, the MGE parametrization of the intrinsic light profile can be easily and analytically recovered

for a choice of the inclination angle i. Here, we adopt  $i=60^\circ$ , i.e. the average inclination for random orientations, and, whenever the axial ratio of the Gaussians does not allow deprojection for this inclination, we adopt the minimum inclination permitted. Note that a significant error in the adopted value of i would produce errors smaller than 10 per cent on the retrieved mass-to-light ratio, if the observed axial ratio is q<0.7 (see Cappellari et al. 2006 fig. 4 for a detailed discussion). Given these inputs, with the jam (see footnote 1) method we are able to directly compute the projected second velocity moment along the line of sight  $V_{\rm rms}$ , with a single numerical quadrature. Finally, in order to compare  $V_{\rm rms}$  with  $\sigma_*$ , we convolve it with a Gaussian PSF with an FWHM (full width at half-maximum) of 1.5 arcsec, as typical for SDSS observations, and then we compute a luminosity-weighted average inside the 3 arcsec diameter SDSS fibre.

# 3.1.3 Inferring the parameters of the dynamical models

For each galaxy in the sample, we built a set of galaxy models, whose mass structure and kinematical configuration have been already described in Sections 3.1.1 and 3.1.2, respectively. We then use two observationally derived quantities to constrain the best model: the SDSS-measured aperture stellar velocity dispersion  $\sigma_*$ , provided by the SDSS data base, and the total projected mass  $M_{\rm EIN}$  enclosed within the Einstein ring of radius  $R_{\rm EIN}$ , calculated by Auger et al. (2009). These quantities are reproduced in Table 1 with their errors; for  $M_{\rm EIN}$  we adopt an error of 5 per cent.

Within a set, the models have the same values for  $(M_{\rm BH}, i, \beta_z)$ , and they differ only in the mass normalization of the two main components: the stellar population and the DM halo. In practice, we choose a sufficiently wide range within which the r-band stellar mass-to-light ratio  $(M_*/L)_{\rm dyn}$  is allowed to vary, and we multiply the MGE model surface density by  $(M_*/L)_{dvn}$ ; in this way we convert the MGE model into a mass density. Analogously, we choose a range for the DM mass normalization by using the parameter  $f_{\rm DM}$ , i.e. the DM fraction within a sphere of radius equal to one effective radius  $R_e$ ; obviously  $0 \le f_{\rm DM} \le 1$ . We then build a model for each couple of values  $((M_*/L)_{\rm dyn}, f_{\rm DM})$ , and we choose the best-fitting model by means of chi-squared minimization on the two observables ( $\sigma_*$ ,  $M_{\rm EIN}$ ). The chi-square maps for the whole sample (Fig. 3) show some degeneracy between  $f_{\rm DM}$  and  $(M_*/L)_{\rm dyn}$ . In general, the DM fraction is very low ( $f_{\rm DM} \lesssim 0.4$ ) and for nearly half of the sample it tends to zero, probably due to systematics. Few galaxies are indeed scarcely reproduced by the NFW profile here adopted, probably due to systematic errors associated with  $\sigma_*$ , or to difficulties in the retrieval of the MGE parametrization because of strong lens disturbances, or to the lensing analysis. Table 2 shows the best-fitting  $(M_*/L)_{\rm dyn}$  and  $f_{\rm DM}$ , and reports the associated typical errors. These are the median values of the  $1\sigma$  errors, computed projecting the white areas in Fig. 3 in the allowed region of the parameters.

Isotropic models (not shown here) result overall in lower  $f_{\rm DM}$  and higher  $(M_*/L)_{\rm dyn}$ , which do not affect any of our results. The dynamical contribution of the BH is irrelevant, since removing it from the modelling results in a negligible increase of  $(M_*/L)_{\rm dyn}$ : the percentage variation has a median value of 1 per cent for the whole sample, and is always smaller than 7 per cent.

Finally, we also built another set of dynamical models where the total mass distribution follows that of the light (mass-follows-light models). These are less sophisticated dynamical models that are constrained only using  $\sigma_\ast$ , and whose best-fitting mass-to-light ratios are reported in Table 2 as  $(M/L)_{\rm MFL}$ . The associated typical

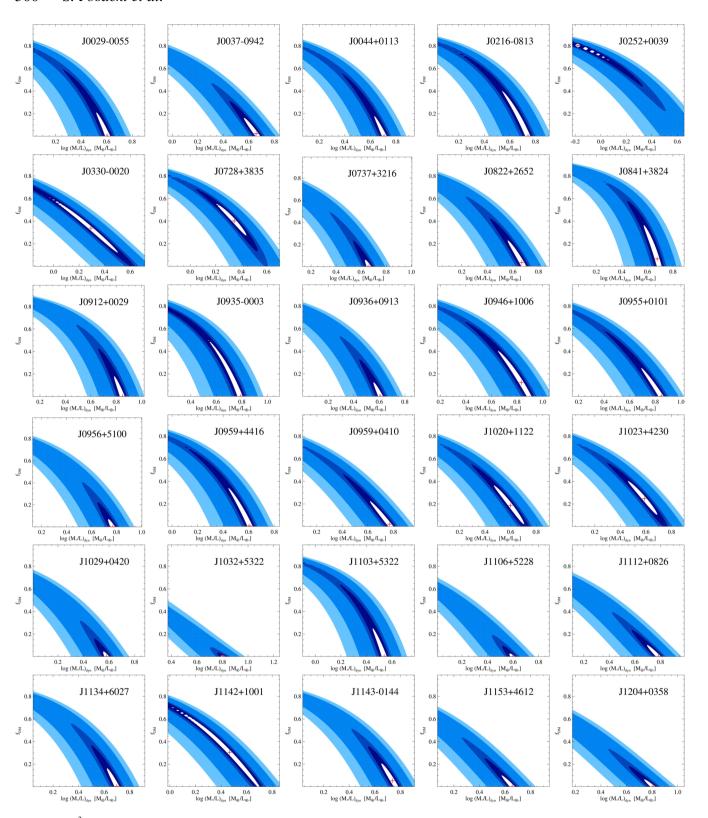


Figure 3.  $\Delta \chi^2$  contour maps obtained from the dynamical models, as a function of the DM fraction  $f_{\rm DM}$  (vertical axis) and r-band stellar mass-to-light ratio  $(M_*/L)_{\rm dyn}$  (horizontal axis). The red cross locates the minimum chi-square value. The 1, 2,  $3\sigma$  confidence levels for 1 degree of freedom ( $\Delta \chi^2 = 1, 4, 9$ ) are shown in white, dark blue and light blue, respectively.

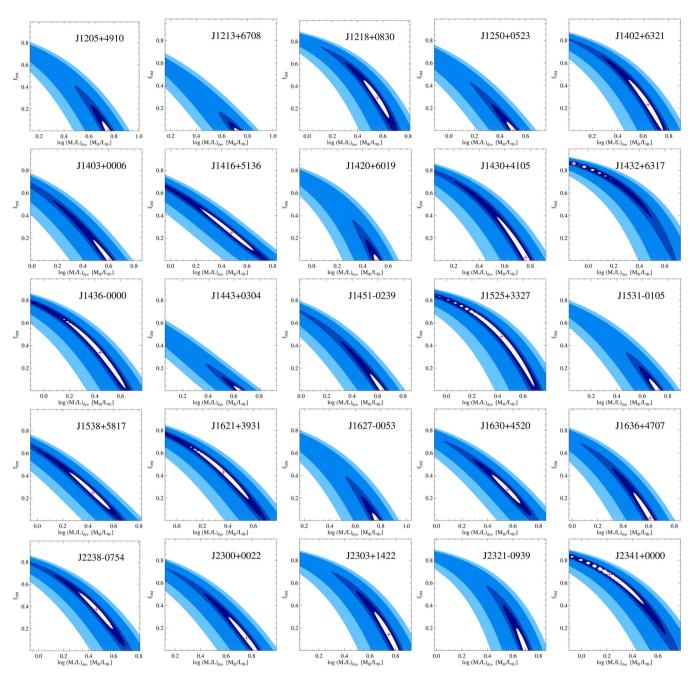


Figure 3 - continued

error is reported in Table 2. It is computed propagating the errors in  $\sigma_*$  and in the jam modelling (6 per cent, as evaluated in Cappellari et al. 2006 from a wider exploration of dynamical modelling approaches), and adopting the median value for all the galaxies.

# 3.2 The stellar population synthesis modelling

Our stellar population synthesis models are performed applying a full-spectrum fitting approach to SDSS spectra, and using a selection of the simple stellar population (SSP) models of Vazdekis et al. (2010),<sup>4</sup> which are based on the MILES stellar spectral

library (Sánchez-Blázquez et al. 2006), and cover the wavelength range 3540–7410 Å at 2.50 Å (FWHM) spectral resolution. In particular, we adopt the Salpeter (1955) IMF as reference, and we select the MILES SSP models with age  $t \ge 1$  Gyr and metallicity  $-1.71 \le [M/H] \le 0.22$ : this leads to a total of 156 SSPs with 26 logarithmically spaced ages, and metallicity values [M/H] = [-1.71, -1.31, -0.71, -0.40, 0.00, 0.22]. For each galaxy then, the spectral fitting is allowed to use only SSPs with age not greater than the age of the Universe at the galaxy redshift, reducing the number of SSP templates to N < 156. The full-spectrum fitting is performed with the PPXF software (see footnote 1), which implements the Penalized Pixel-Fitting method of Cappellari & Emsellem (2004), and, for each galaxy, returns the best-fitting matrix of weights w (to be multiplied by the SSP templates). Then, the stellar mass-to-light

<sup>&</sup>lt;sup>4</sup> Available at http://miles.iac.es/.

**Table 2.** Mass-to-light ratios and  $f_{\rm DM}$  of the models for the 55 galaxy SLACS subsample.

	<i>y y y y y y y y y y</i>			1
Name	$\frac{\log (M/L)_{\text{MFL}}}{(M_{\bigodot}/L_{\bigodot r})}$	$\frac{\log (M_*/L)_{\rm dyn}}{(M_{\bigodot}/L_{\bigodot r})}$	$\log (M_*/L)_{\text{Salp}} $ $(M_{\bigodot}/L_{\bigodot r})$	$f_{\rm DM}$
(1)	(2)	(3)	(4)	(5)
J0029-0055	0.693	0.609	0.610	< 0.207
J0037-0942	0.665	0.648	0.615	0.036
J0044+0113	0.771	0.708	0.642	< 0.174
J0216-0813	0.747	0.737	0.635	< 0.401
J0252+0039	0.439	-0.178	0.646	0.804
J0330-0020	0.487	0.279	0.557	0.350
J0728+3835	0.491	0.331	0.598	0.416
J0737+3216	0.819	0.662	0.572	< 0.061
J0822+2652	0.681	0.665	0.531	0.041
J0841 + 3824	0.688	0.672	0.724	0.079
J0912+0029	0.872	0.848	0.728	< 0.174
J0935-0003	0.923	0.784	0.545	< 0.511
J0936+0913	0.640	0.611	0.600	< 0.123
J0946+1006	0.871	0.824	0.632	0.137
J0955+0101	0.858	0.846	0.640	< 0.246
J0956+5100	0.826	0.765	0.646	< 0.070
J0959+4416	0.631	0.609	0.524	0.003
J0959+0410	0.777	0.763	0.661	0.024
J1020+1122	0.662	0.595	0.634	0.194
J1023+4230	0.674	0.578	0.662	0.256
J1029+0420	0.672	0.581	0.637	< 0.044
J1032+5322	1.004	0.804	0.670	< 0.009
J1103+5322	0.599	0.539	0.690	< 0.246
J1106+5228	0.668	0.593	0.680	< 0.027
J1112+0826	0.793	0.783	0.625	0.001
J1134+6027	0.714 0.624	0.698	0.677	0.001
J1142+1001 J1143-0144	0.754	0.437 0.734	0.665 0.713	0.338 0.060
J1153+4612	0.678	0.656	0.658	0.000
J1204+0358	0.835	0.805	0.677	< 0.065
J1205+4910	0.785	0.751	0.667	< 0.086
J1213+6708	0.817	0.717	0.684	< 0.022
J1218+0830	0.640	0.555	0.667	0.294
J1250+0523	0.548	0.509	0.522	< 0.078
J1402+6321	0.706	0.620	0.661	0.256
J1403+0006	0.656	0.607	0.468	< 0.180
J1416+5136	0.612	0.458	0.575	0.265
J1420+6019	0.596	0.513	0.649	< 0.055
J1430+4105	0.774	0.755	0.640	0.044
J1432+6317	0.569	-0.112	0.658	0.862
J1436-0000	0.588	0.440	0.652	0.338
J1443+0304	0.686	0.647	0.594	< 0.040
J1451-0239	0.679	0.635	0.579	< 0.146
J1525+3327	0.622	0.433	0.612	0.478
J1531-0105	0.728	0.720	0.706	< 0.103
J1538+5817	0.577	0.429	0.671	0.256
J1621+3931	0.571	0.365	0.629	0.431
J1627-0053	0.830	0.766	0.653	< 0.065
J1630+4520	0.671	0.555	0.685	0.275
J1636+4707	0.620	0.608	0.639	0.030
J2238-0754	0.621	0.461	0.631	0.375
J2300+0022	0.804	0.754	0.661	0.115
J2303+1422	0.779	0.744	0.691	0.147
J2321-0939	0.709	0.700	0.657	0.001
J2341+0000	0.616	0.219	0.470	0.676

Notes: (1) Galaxy name. (2) Total mass-to-light ratio of the mass-follows-light dynamical models (Section 3.1) in the r band (1 $\sigma$  error of 14 per cent or 0.056 dex). (3) and (4) r-band stellar mass-to-light ratios derived from the dynamical and the stellar population synthesis models, respectively (Sections 3.1 and 3.2). The 1 $\sigma$  error in ( $M_*/L$ )<sub>dyn</sub> is 28 per cent (0.106 dex), and 7 per cent (0.03 dex) for ( $M_*/L$ )<sub>Salp</sub>. (5) DM fraction enclosed within a sphere of radius  $R_e$ , derived from the dynamical models (1 $\sigma$  error of 0.16).

ratio in the r band associated with the population model is

$$(M_*/L)_{\text{Salp}} = \frac{\sum_{j=1}^{N} w_j M_j^{\text{nogas}}}{\sum_{j=1}^{N} w_j L_{j,r}},$$
 (2)

where  $M_j^{\text{nogas}}$  and  $L_{j,r}$  are the stellar mass (including neutron stars and BHs, but excluding the gas lost by the stars during stellar evolution) and the r-band luminosity of the jth SSP, respectively. In general, for these unregularized fits, we find that  $N \leq 5$ , and in most of the cases N=2 with the older and more metal rich SSP having  $w \simeq 1$ .

The spectral fitting has been performed also using the PPXF keyword REGUL: in this way the fitting procedure is forced to apply a linear regularization to the weights (see equation 18.5.10 of Press et al. 1992), obtaining a smoother solution than the unregularized fit. The regularized solution is as statistically good as the unregularized one, being still consistent with the observations, but it is more physically plausible and representative of the galaxy population since it reduces the scatter in the retrieved population parameters (i.e. age and metallicity) of the solution. The regularized  $(M_*/L)_{Salp}$ slightly underestimate the unregularized ones by 0.02 dex, with an rms scatter of 0.014 dex; this would imply errors of 7 per cent in the individual  $(M_*/L)_{Salp}$ . Finally, we find that our results are robust against plausible variations of the REGUL parameter, so that here we present the results obtained with the regularized solutions. In both fits we make use of a 10th degree multiplicative Legendre polynomial to correct the continuum shape for calibration effects and account for possible intrinsic dust absorption. The best-fitting  $(M_*/L)_{\text{Salp}}$  are reported in Table 2 for each galaxy.

## 4 RESULTS

Here, we present our main results regarding the mass-to-light ratios we derived and their correlation with the stellar velocity dispersion (M/L– $\sigma$  relation), and we focus mostly on the implications concerning the IMF normalization.

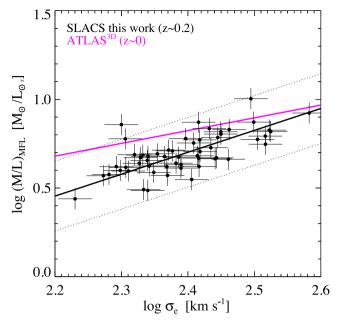
# 4.1 Mass-follows-light models

We recall that these models have a total mass profile that follows that of the light, and are tuned to reproduce only the galaxy surface brightness and the SDSS-measured aperture velocity dispersion. Fig. 4 shows the mass-to-light ratios  $(M/L)_{\rm MFL}$  we derived for these dynamical models as a function of  $\sigma_{\rm e}$ , and the black line is the  $M/L-\sigma_{\rm e}$  relation we obtained for the SLACS sample. The relation is of the form

 $\log(M/L)_r = (1.24 \pm 0.14)$ 

$$\times \log \left( \frac{\sigma_{\rm e}}{200 \,{\rm km \, s^{-1}}} \right) + (0.58 \pm 0.02),$$
 (3)

and has an rms scatter of 0.08 dex. The best-fitting relation has been obtained using the LTS\_LINEFIT routine (see footnote 1) of Cappellari et al. (2013a), which allows and fits for intrinsic scatter, and robustly manages the presence of outliers. In the fit, we consider a typical error of 6 per cent for  $\sigma_e$ , and we quadratically coadded jam modelling errors of 14 per cent, plus distance errors, plus 5 per cent errors for our photometry. When compared with previous similar estimates for different samples of ETGs, local and not (e.g. Cappellari et al. 2006, 2013a; van der Marel & van Dokkum 2007), our relation is slightly steeper. For example, analogous massfollows-light models have been built also for the atlas  $^{3D}$  (Cappellari et al. 2013a) and SAURON samples (Cappellari et al. 2006), leading



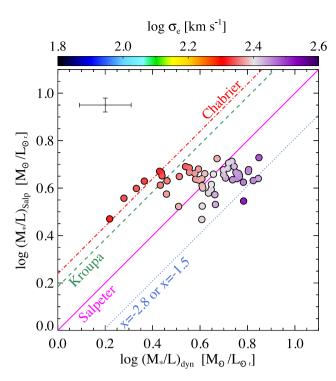
**Figure 4.** *r*-band mass-to-light ratios of the mass-follows-light dynamical models for the SLACS sample, as a function of  $\sigma_e$ , and their best-fitting relation (black line). The magenta line is the best-fitting relation for the atlas<sup>3D</sup> sample (Cappellari et al. 2013a). The values of  $\sigma_e$  are computed as described at the end of Section 3.1.1. Our best-fitting relation is obtained with LTS\_LINEFIT, and the dotted lines mark the  $3\sigma$  bands (enclosing 99.7 per cent of the values for a Gaussian distribution). Outliers deviating more than  $3\sigma$  from the best-fitting relation were automatically excluded from the fit (i.e. points beyond the dotted lines).

to  $M/L-\sigma_{\rm e}$  relations shallower than our, and with higher zero-points (e.g. see the magenta line in Fig. 4). The atlas<sup>3D</sup> sample consists of local galaxies, while the SLACS galaxies reside at higher redshifts (the median redshift for the SLACS sample is  $z \simeq 0.2$ ), so that their stellar populations are younger on average, resulting in lower stellar mass-to-light ratios. Indeed, the offset between the two samples can be accounted just by considering passive evolution. For reference, a solar metallicity ([Z/H] = 0) passively evolving stellar population varies its  $M/L_r$  by  $\sim 0.10$  dex from an age of 11-14 Gyr ( $z \sim 0.2$  to z = 0, assuming it formed at  $z_{\rm form} = \infty$ ), according to the models of Maraston (2005). This value provides a lower limit to the expected passive  $M/L_r$  variation we should observe.

A possible explanation for the steeper slope, instead, could be provided by indications that the  $M/L-\sigma_e$  relation might steepen at the high- $\sigma_e$  end (Zaritsky, Gonzalez & Zabludoff 2006). In fact, the SLACS sample consists mostly of high velocity dispersion galaxies (200 km s $^{-1}\lesssim\sigma_e\lesssim400$  km s $^{-1}$ ) due to its selection criteria, while for example the volume-limited atlas $^{3D}$  sample extends from high-intermediate  $\sigma_e$  galaxies to very low  $\sigma_e$  systems (50 km s $^{-1}\lesssim\sigma_e\lesssim250$  km s $^{-1}$ ). Thus, the two relations shown in Fig. 4 have been obtained sampling different ranges in velocity dispersion, that barely intersect each other.

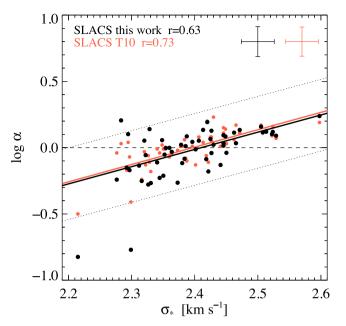
# 4.2 Dependence of the IMF normalization on velocity dispersion

Fig. 5 shows the two sets of stellar mass-to-light ratios obtained from our dynamical and stellar population synthesis models, one against the other. Note that, at variance with  $(M/L)_{\rm MFL}$ , the dynamical mass-to-light ratios  $(M_*/L)_{\rm dyn}$  here shown are purely stellar, since a NFW DM halo has been included in the modelling, so that



**Figure 5.** The stellar mass-to-light ratios  $(M_*/L)_{\rm Salp}$  for a Salpeter IMF (Section 3.2) are shown as a function of the dynamical stellar mass-to-light ratios  $(M_*/L)_{\rm dyn}$  (Section 3.1), both derived in the r band. The colours of the symbols code the galaxy velocity dispersion: in place of the individual  $\sigma_{\rm e}$  values, here we show the two-dimensional loess-smoothed  $\sigma_{\rm e}$  values (see the top colour bar). A representative error bar is shown at the top-left. Two galaxies resulting in too high and unrealistic DM fractions (J0252+0039 and J1432+6317) have been excluded from the plot. The diagonal lines are computed from the Vazdekis et al. (2010) models for a population with solar metallicity.

they can be directly compared with  $(M_*/L)_{\rm Salp}$ . Thus, if for example the IMF of ETGs is universal and Salpeter-like,  $(M_*/L)_{\rm dyn}$  should be very similar to  $(M_*/L)_{Salp}$ , which has been calculated under this assumption (i.e. all galaxies should lie close to the magenta line, with some scatter). If otherwise ETGs have a lighter IMF, like Chabrier or Kroupa, one would expect to find that  $(M_*/L)_{Salp}$  systematically overestimates  $(M_*/L)_{\rm dyn}$  by the same percentage, for the whole sample. The situation apparent in Fig. 5 is somewhat different: galaxies do not lie near one of the lines representing different IMFs, but are distributed across all of them. The scatter is significant compared to the typical error, and reveals that some galaxies are actually more properly represented by a lighter or a heavier IMF normalization. This suggests a variation of the IMF for ETGs, that seems also to correlate with the galaxy velocity dispersion, with low- $\sigma_e$  galaxies being consistent with a Chabrier or Kroupa-like IMF, while medium and high- $\sigma_e$  galaxies agree with a Salpeter or heavier IMF. Note that our results are equally consistent with both a bottom heavy and top heavy IMF trend (as considered by Weidner et al. 2013), since the approach we use does not constrain the shape of the IMF directly, but only the overall mass normalization. In Fig. 5, each galaxy is coloured according to its loesssmoothed value of  $\sigma_e$ , as done in Cappellari et al. (2013b, their fig. 11). Applying the loess (see footnote 1) method (Cleveland 1979), we evaluated mean values of  $\sigma_e$  that are the result of an average over the neighbouring galaxies, weighted with the relative distances. In this way, one aims to reconstruct the average values characterizing the underlying galaxy population, i.e. the values one



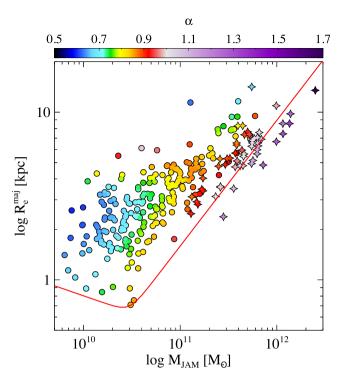
**Figure 6.** IMF mismatch parameter  $\alpha$  as a function of  $\sigma_*$  for the SLACS sample. Red points are taken from T10, as well as their best-fitting relation represented by the red line. Black points refer to the values computed in this work. The black line is our best-fitting relation obtained with LTS\_LINEFIT, and the dotted lines mark the  $3\sigma$  bands (enclosing 99.7 per cent of the values for a Gaussian distribution). Outliers deviating more than  $3\sigma$  from the best-fitting relation were automatically excluded from the fit (i.e. points beyond the dotted lines). The value of the linear correlation coefficient r is also reported. Representative error bars are shown at the top-right: for the data of T10 we compute the median error.

should expect to obtain when disposing of much larger galaxy samples.

Another way of seeing this variation is by looking at the IMF mismatch parameter  $\alpha \equiv (M_*/L)_{\rm dyn}/(M_*/L)_{\rm Salp}$ . Fig. 6 shows the logarithm of  $\alpha$  as a function of  $\sigma_*$ , as already done in T10 (see their fig. 4, central panel). Here, the red points refer to the values obtained by T10, while our results are shown in black, and the solid lines are the respective best-fitting relations. Note that the dynamical models of T10 consist of spherical isotropic models, with a stellar component following a Hernquist (1990) profile. Moreover, their stellar population synthesis models were built using multicolour HST photometry, while ours are based on full-spectrum fitting. Regardless of the very different approaches adopted, we find that the two works produce essentially the same result pointing towards an IMF variation, with high- $\sigma_*$  galaxies being consistent on average with a Salpeter normalization. Our relation is

$$\log \alpha = (1.3 \pm 0.23) \times \log \left( \frac{\sigma_*}{200 \,\mathrm{km \, s^{-1}}} \right) - (0.14 \pm 0.03), \quad (4)$$

with an rms scatter of 0.1 dex; in the fit we consider a median error of 6 per cent for  $\sigma_*$ , and we quadratically co-added the dynamical modelling errors of 28 per cent, plus distance errors, plus population models errors of 7 per cent, plus 5 per cent errors for our photometry. Our relation is very similar to that reported in T10. However, inspecting Fig. 6 a difference must be noted: our dynamical modelling produces a weaker correlation, in the sense that our points are more scattered in the  $(\log \alpha, \sigma_*)$  plane with respect to T10 points. This is reasonably due to the use of a more flexible parametrization of the light profiles. Indeed, given its nature, the SLACS sample is likely to include also compact galaxies, and using a density profile with a



**Figure 7.**  $R_{\rm e}^{\rm maj}$ , the major axis of the isophotes containing half of the analytic total light of the MGE models, is shown as function of  $M_{\rm JAM}$ , the total mass of the mass-follows-light models (i.e.  $M_{\rm JAM} = (M/L)_{\rm MFL} \times L_r$ ), for the SLACS (stars) and atlas<sup>3D</sup> samples (circles). The colours of the symbols code the ratio  $\alpha = (M_*/L)_{\rm dyn}/(M_*/L)_{\rm Salp}$ : in place of the individual  $\alpha$  values, here we show the two-dimensional loess-smoothed  $\alpha$  values (see the top colour bar). The red line shows the zone of exclusion relation given by equation 4 of Cappellari et al. (2013b), for the atlas<sup>3D</sup> sample.

fixed internal slope (like the Hernquist profile) to fit all the galaxies might artificially produce some correlation, by overestimating the stellar mass in the high- $\sigma_e$  compact galaxies. Fig. 7 illustrates the type of galaxies that are in the  $\sigma$ -selected SLACS sample (stars), compared to the volume-selected atlas<sup>3D</sup> sample (circles): it can be noticed that they are quite massive and dense, since they fill the lower envelope of the galaxy distribution in the  $(R_{\rm e}^{\rm maj}, M_{\rm JAM})$  at the high-mass end (i.e. with the smaller  $R_{\rm e}^{\rm maj}$  for  $M_{\rm JAM} > 10^{11} \, {\rm M}_{\odot}$ ). Finally, the analysis we conducted on the SLACS sample is analogous to the one performed on the atlas<sup>3D</sup> sample, both in terms of the dynamical and stellar population approach. This allows us to directly compare the respective results, and merge the two samples homogeneously analysed to infer some global insights on the IMF of ETGs. Fig. 8 shows the IMF mismatch parameter as a function of  $\sigma_e$  for the two samples (i.e. SLACS in black and atlas<sup>3D</sup> in magenta). Here, notwithstanding the heterogeneity of the samples in terms of selection criteria, galaxy redshift and mass range, one can immediately appreciate how the black points seem to follow the same relation of the magenta points, but extending to higher  $\sigma_e$  values. Indeed, the magenta solid line, representing the best-fitting relation for the atlas<sup>3D</sup> sample, is only slightly shallower that the blue solid line, obtained by fitting both samples together; in particular, we find for the whole sample SLACS + atlas<sup>3D</sup>

$$\log \alpha = (0.38 \pm 0.04) \times \log \left( \frac{\sigma_{\rm e}}{200 \,\mathrm{km \, s^{-1}}} \right) + (-0.06 \pm 0.01), \tag{5}$$

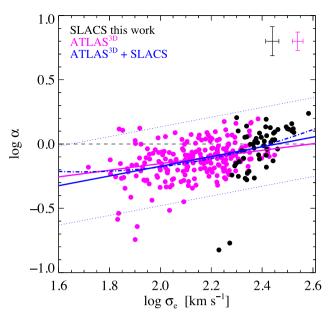


Figure 8. The IMF mismatch parameter  $\alpha$  is shown as a function of  $\sigma_e$  for the SLACS (black) and the atlas<sup>3D</sup> sample (magenta). The magenta solid line is the best-fitting relation for the subset of the whole atlas<sup>3D</sup> sample made of 223 galaxies with the stellar absorption line-strength index  $H\beta < 2.3$  Å, taken from Cappellari et al. (2013b). The blue solid line is the best-fitting relation for the two samples put together, obtained with LTS\_LINEFIT, and the blue dotted lines mark the  $3\sigma$  bands (enclosing 99.7 per cent of the values for a Gaussian distribution). Outliers deviating more than  $3\sigma$  from the best-fitting relation were automatically excluded from the fit (i.e. points beyond the dotted lines). The blue dot–dashed line is a parabolic fit to both samples together, performed with the MPFITTUN routine. Representative error bars are shown at the top-right: for the data of Cappellari et al. (2013b), we compute the median error.

with an rms scatter of 0.12 dex. The similarity of the two best-fitting relations is even more remarkable when comparing them with the steeper relation we find for the SLACS sample alone (equation 4). Note that the steepness of the slope in equation (4) is not due to the fact that  $\alpha$  is fitted as a function of  $\sigma_*$  instead of  $\sigma_e$ , since we find a very similar result also for  $\sigma_e$  (slightly steeper). This shows that the slope of the  $\alpha-\sigma_e$  relation is very sensitive to the  $\sigma_e$  range, with a considerable increase for  $\sigma_e\gtrsim 250\,\mathrm{km\,s^{-1}}$ , and suggests that the relation is not a simple single power law. In this scenario, the steepness of the  $\alpha-\sigma_e$  correlation, found by T10 and confirmed here, for the ETGs of the SLACS sample is a natural consequence of the velocity dispersion selection nature of the SLACS sample. We then try to fit a parabola to the whole sample SLACS + atlas^{3D}, obtaining

$$\log \alpha = (0.40 \pm 0.15) \times \log \left(\frac{\sigma_{\rm e}}{200 \,\mathrm{km \, s^{-1}}}\right)^{2} + (0.49 \pm 0.05) \times \log \left(\frac{\sigma_{\rm e}}{200 \,\mathrm{km \, s^{-1}}}\right) + (-0.07 \pm 0.01), \tag{6}$$

with an rms scatter of 0.12 dex.

Thus, by homogeneously studying ETGs collected over a very wide and unprecedented range of  $\sigma_{\rm e}$  and  $M_*$ , we have provided a comprehensive insight about the IMF normalization for this morphological type of galaxies, showing that the IMF gets heavier for increasing  $\sigma_{\rm e}$ , and becomes Salpeter-like at  $\sigma_{\rm e} \simeq 250\,{\rm km\,s^{-1}}$ . The issue of the IMF variability for the atlas<sup>3D</sup> sample has also been

studied by Tortora et al. (2014) within the Modified Newtonian Dynamics (MOND) framework, obtaining results consistent with the ones from Newtonian dynamics plus DM.

# 5 DISCUSSION AND CONCLUSIONS

In this work, we studied the mass normalization of the IMF of ETGs, exploiting information derived from gravitational lensing, stellar dynamics and stellar population synthesis models, and making use of high-quality photometric and spectroscopic data. We selected 55 ETGs belonging to the SLACS sample and constructed dynamical and stellar population synthesis models for each galaxy. Our dynamical models are built solving the Jeans axisymmetric anisotropic equations with the jam method of Cappellari (2008); they reproduce in detail the *HST* galaxy images and are constrained using the SDSS-measured velocity dispersion and the mass within the Einstein radius. Our stellar population synthesis models are computed with the full-spectrum fitting technique and are based on the SSP models of Vazdekis et al. (2010). We derived accurate estimates of stellar mass-to-light ratios from the two sets of models,  $(M_*/L)_{\rm dyn}$  and  $(M_*/L)_{\rm Salp}$ , respectively.

From the comparison of the two estimates of stellar mass-to-light ratios, we find a trend of IMF with velocity dispersion, where, on average, the IMF normalization smoothly varies from Kroupa/Chabrier for galaxies with  $\sigma_e \sim 90~km~s^{-1}$ , up to a bottom-heavy Salpeter-like IMF for galaxies with  $\sigma_e \sim 270~km~s^{-1}$  (Fig. 5). This change of IMF normalization as a function of  $\sigma_e$  is significant beyond the extent of the error estimates in the stellar the mass-to-light ratios, and thus suggests an intrinsic systematic variation of the stellar IMF for ETGs.

With our accurate and realistic modelling of the stellar profiles, our analysis provides an improvement over the study of T10, conducted on the same ETG sample. Notwithstanding the different and independent approaches adopted, we confirm their finding of a steep correlation between the IMF mismatch parameter  $\alpha = (M_*/L)_{\rm dyn}/(M_*/L)_{\rm Salp}$  and the galaxy velocity dispersion (Fig. 6); however, our relation has a slightly lower correlation coefficient, presumably due to relaxing the restrictive assumption of a fixed stellar density profile to fit the whole galaxy sample.

We also built mass-follows-light dynamical models and computed total mass-to-light ratios  $(M/L)_{\rm MFL}$  for them. We find an  $(M/L)_{\rm MFL}$ - $\sigma_{\rm e}$  correlation steeper than previous analogous estimates for different local ETG samples (e.g. the  $(M/L)_{\rm MFL}$ - $\sigma_{\rm e}$  relation for the 260 ETGs atlas<sup>3D</sup> sample), and with a lower zero-point (Fig. 4). The SLACS sample resides at higher redshift and is likely to include galaxies with younger stellar populations; indeed, the offset in the zero-points can be accounted for by passive evolution between  $z\sim0.2$  and z=0. The different slope instead could be an effect of the different  $\sigma_{\rm e}$  range spanned by the samples, in accordance with Zaritsky et al. (2006) that suggests a steepening this relation as a function of  $\sigma_{\rm e}$ . Note that the slope of the  $(M/L)_{\rm MFL}$ - $\sigma_{\rm e}$  relation gives an upper limit to any systematic increase of the IMF mass normalization with  $\sigma_{\rm e}$ .

Finally, as an important outcome of analysing the SLACS galaxies with a procedure that is homogeneous with that adopted for the atlas<sup>3D</sup> galaxies (Cappellari et al. 2013b), we could merge the two samples. In this way, we explored the behaviour of ETGs in the  $\alpha$ –  $\sigma_e$  plane with the largest sample ever, where ETGs of all  $\sigma_e$  values from 50 to  $\sim$ 350 km s<sup>-1</sup> are well represented. We found that the volume-limited atlas<sup>3D</sup> sample and the velocity dispersion selected SLACS galaxies smoothly merge in a unique shallower relation in the  $(\alpha, \sigma_e)$  plane (Fig. 8). From this comprehensive analysis, we

find that the  $\alpha-\sigma_e$  relation might not be linear, and that the slope inferred depends on the range of  $\sigma_e$  covered by the galaxies. This is significantly different for the atlas<sup>3D</sup> (volume selected) and SLACS sample (velocity dispersion selected).

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# APPENDIX A: MGE MODEL PARAMETERS

For each galaxy, the parameters of the best-fitting MGE parametrizations of the projected light are presented in Table A1.

**Table A1.** MGE parameters for the deconvoled r-band surface brightness.

$\log I_i \atop (L_{\bigodot r} \operatorname{pc}^{-2})$	$\log \sigma_i$ (arcsec)	$q_i$	$\log I_i  (L_{\bigodot r} \operatorname{pc}^{-2})$	$\log \sigma_i$ (arcsec)	$q_i$	$\log I_i  (L_{\bigodot r} \operatorname{pc}^{-2})$	$\log \sigma_i$ (arcsec)	$q_i$	$\log I_i  (L_{\bigodot_r} \operatorname{pc}^{-2})$	$\log \sigma_i$ (arcsec)	$q_i$
J0029-0055		J00	37–0942		J00	44+0113		J02			
3.895	-1.532	0.922	3.124	-1.323	0.891	3.552	-1.264	0.693	3.392	-1.532	0.842
3.700	-1.050	0.941	3.442	-0.924	0.693	3.735	-0.786	0.567	3.536	-1.006	0.842
3.372	-0.684	0.903	3.494	-0.773	0.693	3.507	-0.565	0.820	3.454	-0.762	0.842
2.714	-0.183	0.792	3.355	-0.496	0.693	2.549	-0.209	0.554	3.183	-0.450	0.794
1.902	-0.076	0.941	3.068	-0.212	0.693	2.871	-0.113	0.842	2.718	-0.126	0.792
2.081	0.174	0.792	2.225	0.127	0.891	2.422	0.193	0.842	2.377	0.171	0.792
1.677	0.570	0.838	2.356	0.152	0.693	1.521	0.304	0.297	1.935	0.531	0.842
			1.833	0.593	0.891	1.018	0.658	0.297			
						1.820	0.658	0.758			
J0252+0039		J03	J0330-0020			J0728+3835			J0737+3216		
4.005	- 1.532	0.941	4.247	- 1.532	0.787	4.156	-1.532	0.845	3.631	- 1.532	0.941
3.462	-1.078	0.941	3.215	-1.094	0.745	3.811	-1.069	0.852	3.778	-1.119	0.982
3.240	-0.724	0.941	3.670	-0.925	0.829	3.583	-0.790	0.838	3.474	-0.700	0.900
2.199	-0.143	0.652	3.028	-0.601	0.842	3.125	-0.521	0.941	2.880	-0.188	0.990
2.684	-0.136	0.941	2.679	-0.406	0.743	2.670	-0.303	0.512	2.317	0.142	0.842
1.834	0.212	0.941	2.529	-0.111	0.743	2.698	-0.044	0.746	1.815	0.552	0.842
			1.976	-0.055	0.842	2.089	0.183	0.792			
			1.949	0.300	0.835	1.484	0.541	0.495			
						1.568	0.541	0.804			
J0822+2652		J084	41+3824			J0912+0029			J0935-0003		
3.935	-1.532	0.792	4.318	-1.532	0.760	3.349	-1.433	0.801	3.459	-1.162	0.862
3.676	-1.074	0.792	3.810	-0.996	0.990	3.464	-0.917	0.870	3.499	-0.848	0.822

Table A1 - continued

$\log I_i \atop (L_{\bigodot r} \operatorname{pc}^{-2})$	$\log \sigma_i$ (arcsec)	$q_i$	$\log I_i  (L_{\bigodot r} \operatorname{pc}^{-2})$	$\log \sigma_i$ (arcsec)	$q_i$	$\log I_i  (L_{\bigodot r} \operatorname{pc}^{-2})$	$\log \sigma_i$ (arcsec)	$q_i$	$\log I_i  (L_{\bigodot r} \operatorname{pc}^{-2})$	$\log \sigma_i$ (arcsec)	$q_i$
3.536	- 0.796	0.792	3.056	- 0.551	0.531	3.097	- 0.629	0.732	3.276	- 0.570	0.823
3.173	-0.470	0.743	3.296	-0.423	0.792	3.172	-0.410	0.727	2.819	-0.247	0.862
2.713	-0.118	0.792	2.878	-0.142	0.848	2.520	-0.092	0.565	2.371	0.058	0.862
2.186	0.177	0.759	2.202	0.278	0.446	2.680	0.029	0.597	2.129	0.532	0.862
1.791	0.528	0.743	2.249	0.493	0.446	2.329	0.047	0.941			
			1.598	0.937	0.798	2.120	0.392	0.841			
						2.053	0.427	0.443			
						1.584	0.826	0.657			
J093	36+0913		J094	46+1006		J09.	55+0101		J09	56+5100	
4.075	-1.532	0.822	3.338	-1.532	0.990	4.135	-1.532	0.720	3.818	-1.532	0.743
3.780	-1.019	0.818	3.374	-0.940	0.990	3.634	-1.064	0.599	3.827	-1.025	0.743
3.437	-0.800	0.826	3.250	-0.568	0.990	3.286	-0.772	0.842	3.496	-0.751	0.743
3.233	-0.506	0.828	2.587	-0.023	0.990	2.841	-0.520	0.842	3.236	-0.504	0.743
2.574	-0.270	0.842	1.475	0.287	0.743	2.878	-0.036	0.248	2.679	-0.024	0.743
2.467	-0.060	0.792	1.642	0.585	0.743	2.459	0.116	0.411	2.353	0.040	0.941
2.342	0.198	0.817				1.324	0.396	0.842	1.760	0.268	0.743
1.706	0.584	0.833				1.630	0.396	0.442	1.791	0.579	0.743
J09:	59+4416		J09:	59+0410		J10	20+1122		J10	23+4230	
3.272	-1.253	0.941	4.098	-1.532	0.801	3.731	-1.413	0.792	4.322	-1.532	0.866
3.593	-1.018	0.941	3.523	-1.123	0.857	3.811	-0.967	0.792	3.781	-1.026	0.891
3.429	-0.748	0.877	3.466	-0.866	0.746	3.444	-0.656	0.792	3.230	-0.754	0.842
3.079	-0.492	0.892	3.062	-0.525	0.847	2.989	-0.374	0.792	3.149	-0.517	0.842
2.726	-0.185	0.941	2.582	-0.025	0.891	2.656	-0.033	0.803	2.668	-0.179	0.842
1.756	0.178	0.492	2.273	0.142	0.383	1.930	0.348	0.990	2.446	0.074	0.891
2.136	0.184	0.879	1.852	0.299	0.714				1.766	0.490	0.883
1.676	0.507	0.865									
J10:	29+0420		J10	32+5322		J11	03+5322		J11	06+5228	
4.279	-1.532	0.736	4.256	-1.532	0.827	3.779	-1.532	0.744	4.608	-1.532	0.644
3.788	-0.998	0.758	3.805	-0.991	0.842	3.501	-1.012	0.812	3.928	-0.975	0.743
3.493	-0.715	0.714	3.450	-0.660	0.812	3.369	-0.622	0.677	3.734	-0.961	0.545
3.125	-0.454	0.821	2.745	-0.298	0.813	3.057	-0.083	0.347	3.710	-0.741	0.743
2.962	-0.195	0.396	2.789	-0.038	0.297	2.228	0.020	0.842	2.948	-0.580	0.545
2.065	0.075	0.891	2.327	0.188	0.348	2.441	0.234	0.347	3.459	-0.482	0.743
2.622	0.094	0.396	1.288	0.390	0.842	1.918	0.312	0.574	2.785	-0.240	0.545
2.198	0.299	0.504	1.577	0.390	0.297	1.369	0.555	0.447	2.941	-0.020	0.626
1.411	0.517	0.513				1.314	0.555	0.842	1.996	0.279	0.743
1.502	0.517	0.891							2.211	0.350	0.545
									1.787	0.678	0.723
J11	12+0826		J111	34+6027		J11-	42+1001		J11	43-0144	
3.734	-1.240	0.792	4.047	-1.532	0.743	3.710	-1.532	0.990	3.350	-0.792	0.832
3.535	-0.763	0.743	3.784	-0.920	0.743	3.692	-1.059	0.990	3.507	-0.515	0.743
3.070	-0.630	0.743	3.346	-0.597	0.743	3.403	-0.771	0.990	3.213	-0.228	0.743
3.099	-0.368	0.743	3.045	-0.348	0.820	2.928	-0.495	0.990	2.732	0.156	0.753
2.689	-0.072	0.755	2.387	0.012	0.743	2.690	-0.221	0.990	2.095	0.436	0.891
2.142	0.325	0.792	2.218	0.226	0.879	2.105	0.176	0.771	1.507	0.919	0.813
			1.522	0.674	0.891	1.812	0.527	0.743			
J11:	53+4612		J120	04+0358		J12	05+4910		J12	13+6708	
4.166	-1.532	0.842	4.089	-1.532	0.891	3.819	-1.532	0.842	4.345	-1.532	0.857
3.857	-1.027	0.842	3.766	-0.950	0.891	3.386	-1.139	0.842	4.110	-1.052	0.822
3.353	-0.742	0.842	3.275	-0.614	0.891	3.678	-0.921	0.842	3.635	-0.729	0.891
2.869	-0.527	0.842	2.778	-0.347	0.936	3.134	-0.628	0.842	3.170	-0.424	0.880
2.637	-0.381	0.990	2.533	-0.038	0.990	2.923	-0.433	0.693	2.744	-0.007	0.779
2.588	-0.112	0.990	1.992	0.345	0.990	2.732	-0.157	0.842	2.147	0.301	0.799
1.852	0.391	0.842				2.371	0.195	0.693	1.702	0.417	0.693
						1.732	0.589	0.693	1.647	0.805	0.693
						0.827	0.589	0.842			
I12	18+0830		112	50+0523			02+6321		I14	03+0006	
	- 1.532	0.792	4.417	-1.532	0.990	3.875	-1.532	0.792	4.177	-1.532	0.891
	1.002	J.172	1/			5.075				1.332	
3.347	-1.031	0.792	3 871	-0.994	0.990	3 316	-1.058	0.842	3 638	-1.054	0.891
3.347 3.260	-1.031 $-0.805$	0.792	3.871 3.400	-0.994 $-0.591$	0.990	3.316 3.537	-1.058 $-0.858$	0.842	3.638 3.283	-1.054 $-0.680$	0.891
3.347	-1.031 $-0.805$ $-0.542$	0.792 0.792 0.693	3.871 3.400 2.818	-0.994 $-0.591$ $-0.157$	0.990 0.990 0.990	3.316 3.537 3.267	-1.058 $-0.858$ $-0.603$	0.842 0.743 0.743	3.638 3.283 1.979	-1.054 $-0.680$ $-0.250$	0.891 0.891 0.693

Table A1 - continued

	commuca										
$\log I_i \atop (L_{\bigodot r} \operatorname{pc}^{-2})$	$\log \sigma_i$ (arcsec)	$q_i$	$\log I_i  (L_{\bigodot r} \operatorname{pc}^{-2})$	$\log \sigma_i$ (arcsec)	$q_i$	$\log I_i  (L_{\bigodot r} \operatorname{pc}^{-2})$	$\log \sigma_i$ (arcsec)	$q_i$	$\log I_i  (L_{\bigodot_r} \operatorname{pc}^{-2})$	$\log \sigma_i$ (arcsec)	$q_i$
2.668	-0.075	0.693	1.675	0.503	0.772	2.707	-0.059	0.796	2.197	0.174	0.709
2.453	0.175	0.792				2.193	0.263	0.766	1.790	0.384	0.693
1.807	0.475	0.720				1.751	0.619	0.842			
1.530	0.801	0.707									
J14	16+5136		J14	20+6019		J14:	30+4105		J14:	32+6317	
3.661	-1.531	0.973	4.194	-1.532	0.743	3.902	-1.532	0.936	3.914	-1.532	0.976
3.656	-1.039	0.990	3.936	-0.983	0.743	3.709	-0.998	0.941	3.634	-0.994	0.974
3.296	-0.732	0.956	3.486	-0.671	0.743	3.404	-0.595	0.932	3.350	-0.678	0.978
3.111	-0.352	0.794	3.384	-0.501	0.396	2.820	0.071	0.941	2.912	-0.358	0.907
2.389	0.070	0.743	3.471	-0.219	0.396	1.707	0.652	0.594	2.732	-0.003	0.953
1.664	0.427	0.743	3.024	-0.050	0.743				2.182	0.503	0.990
1.090	0.427	0.990	2.435	0.172	0.396				0.158	0.811	0.396
			2.176	0.299	0.743				1.435	0.811	0.990
			2.031	0.452	0.436						
			1.851	0.683	0.716						
J14	136-0000		J14	43+0304		J14	51-0239		J15	25+3327	
3.317	-1.532	0.792	4.369	-1.532	0.792	4.236	-1.532	0.952	3.969	-1.532	0.770
3.227	-1.094	0.812	3.773	-1.045	0.990	3.756	-1.024	0.984	3.635	-1.030	0.792
3.502	-0.783	0.772	3.462	-1.037	0.594	3.378	-0.645	0.921	3.279	-0.703	0.747
3.125	-0.446	0.772	3.298	-0.774	0.594	2.936	-0.349	0.951	2.854	-0.469	0.594
2.136	-0.054	0.772	3.194	-0.556	0.638	2.613	-0.074	0.990	2.801	-0.186	0.594
2.434	-0.028	0.812	2.738	-0.299	0.594	1.716	0.186	0.297	2.559	0.130	0.671
1.991	0.458	0.772	2.064	-0.039	0.990	2.202	0.213	0.990	1.944	0.574	0.606
			2.453	-0.022	0.594	1.690	0.621	0.990			
			1.748	0.449	0.594						
			1.009	0.449	0.990						
	531–0105			38+5817			21 + 3931			27–0053	
3.782	- 1.532	0.718	4.324	-1.532	0.862	3.815	- 1.443	0.767	3.864	- 1.532	0.817
3.753	- 0.949	0.743	3.785	- 0.991	0.862	3.546	- 1.101	0.792	3.417	- 1.144	0.792
3.444	- 0.699	0.693	3.393	-0.620	0.862	3.537	-0.910	0.743	3.627	-0.937	0.843
3.216	-0.480	0.693	2.765	-0.212	0.822	3.339	- 0.591	0.743	3.381	- 0.572	0.827
2.997	-0.280	0.693	2.432	0.070	0.852	2.884	- 0.364	0.743	2.724	-0.085	0.792
2.605 2.473	-0.033 $0.201$	0.693 0.743	1.751	0.475	0.853	2.712 1.993	0.003 0.519	0.792 0.755	2.172 1.730	0.125 0.517	0.941 0.926
1.836	0.201	0.743				1.993	0.319	0.733	1.730	0.317	0.920
		0.093	***	26.4505		***					
	30+4520	0.021		36+4707	0.006		238-0754	0.722		00+0022	0.772
3.925	- 1.532	0.831	3.922	- 1.532	0.896	3.998	-1.532	0.733	2.876	- 1.364	0.773
3.796	- 1.044	0.832	3.595	- 0.991	0.941	3.668	-0.925	0.823	3.405	-0.982	0.843
3.443 2.917	-0.648 $-0.309$	0.831 0.842	3.334 2.954	-0.680 $-0.422$	0.852 0.941	2.853 3.234	-0.668 $-0.524$	0.644 0.891	3.280 3.227	-0.710 $-0.513$	0.703 0.833
2.185	-0.309 $-0.164$	0.684	2.365	-0.422 $-0.274$	0.743	2.431	-0.324 -0.279	0.644	2.342	-0.313 -0.218	0.833
2.163	0.019	0.842	2.358	-0.274 $-0.129$	0.743	2.713	-0.279 $-0.072$	0.891	2.456	-0.218 $-0.067$	0.702
2.104	0.019	0.842	2.280	0.030	0.743	2.145	0.257	0.644	2.036	0.031	0.693
1.865	0.132	0.842	1.965	0.030	0.743	1.797	0.627	0.644	1.567	0.424	0.990
1.005	0.476	0.042	1.703	0.777	0.743	1.777	0.027	0.0	1.692	0.424	0.693
123	03+1422		123	21-0939		123.	41+0000		1.072	0.121	0.075
3.356	-1.202	0.743	3.920	-1.532	0.842	3.973	- 1.523	0.754			
3.555	-0.816	0.743	3.682	-0.950	0.842	3.427	-0.766	0.716			
3.276	-0.440	0.698	3.656	-0.632	0.842	3.365	-0.652	0.792			
2.804	-0.023	0.685	3.199	-0.289	0.743	2.432	-0.128	0.495			
2.328	0.309	0.644	2.920	0.030	0.800	2.458	0.036	0.792			
1.774	0.693	0.646	1.896	0.254	0.743	2.311	0.325	0.495			
			2.434	0.422	0.805	1.548	0.369	0.792			
			1.724	0.846	0.776	1.525	0.697	0.792			

Notes. Column 1: logarithm of the Gaussian amplitude. Column 2: logarithm of the Gaussian width. Column 3: axial ratio of the Gaussian.

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