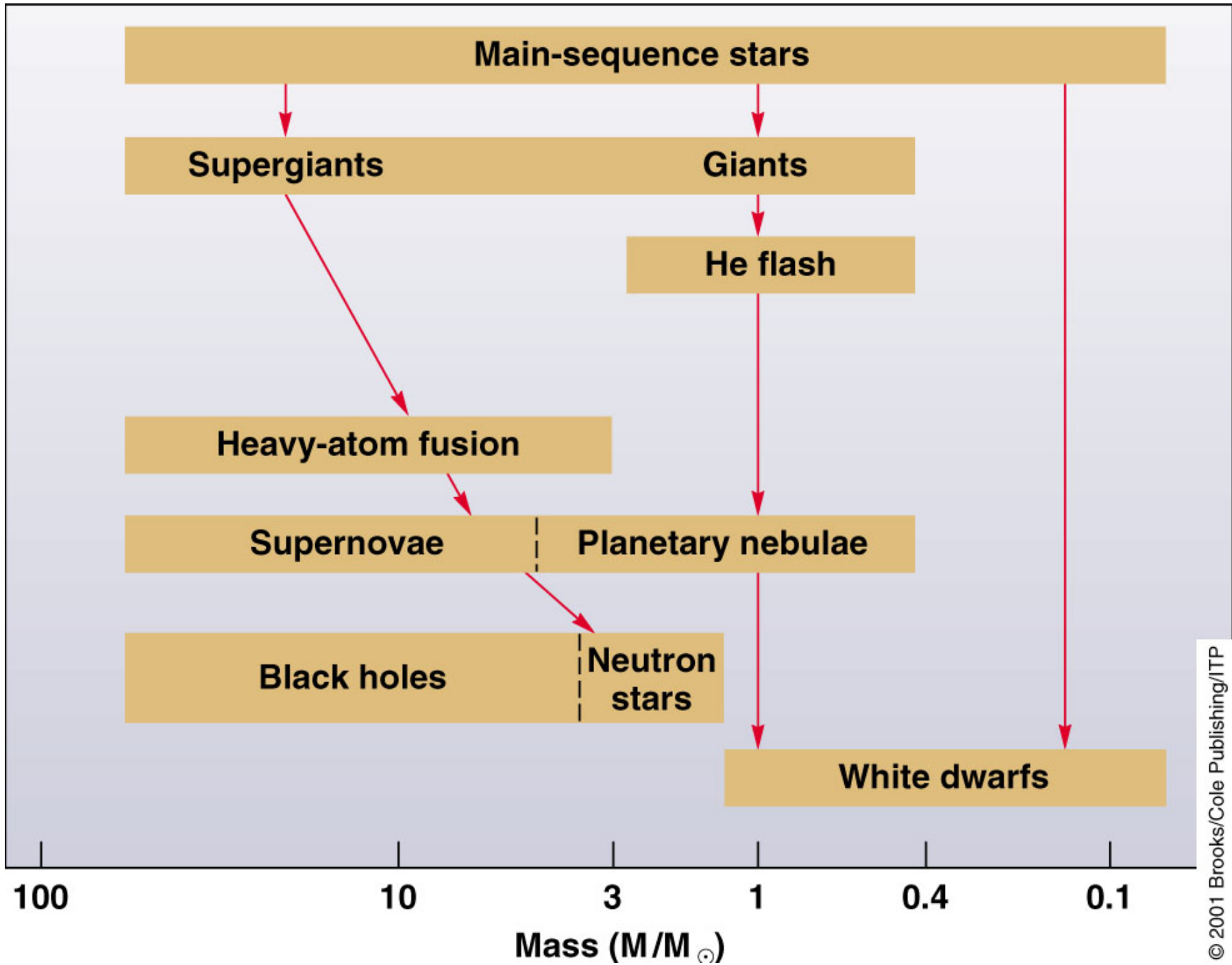


# White dwarfs



# Degenerate objects

In the leftover core of a dead star...

- degeneracy pressure supports the star against the crush of gravity

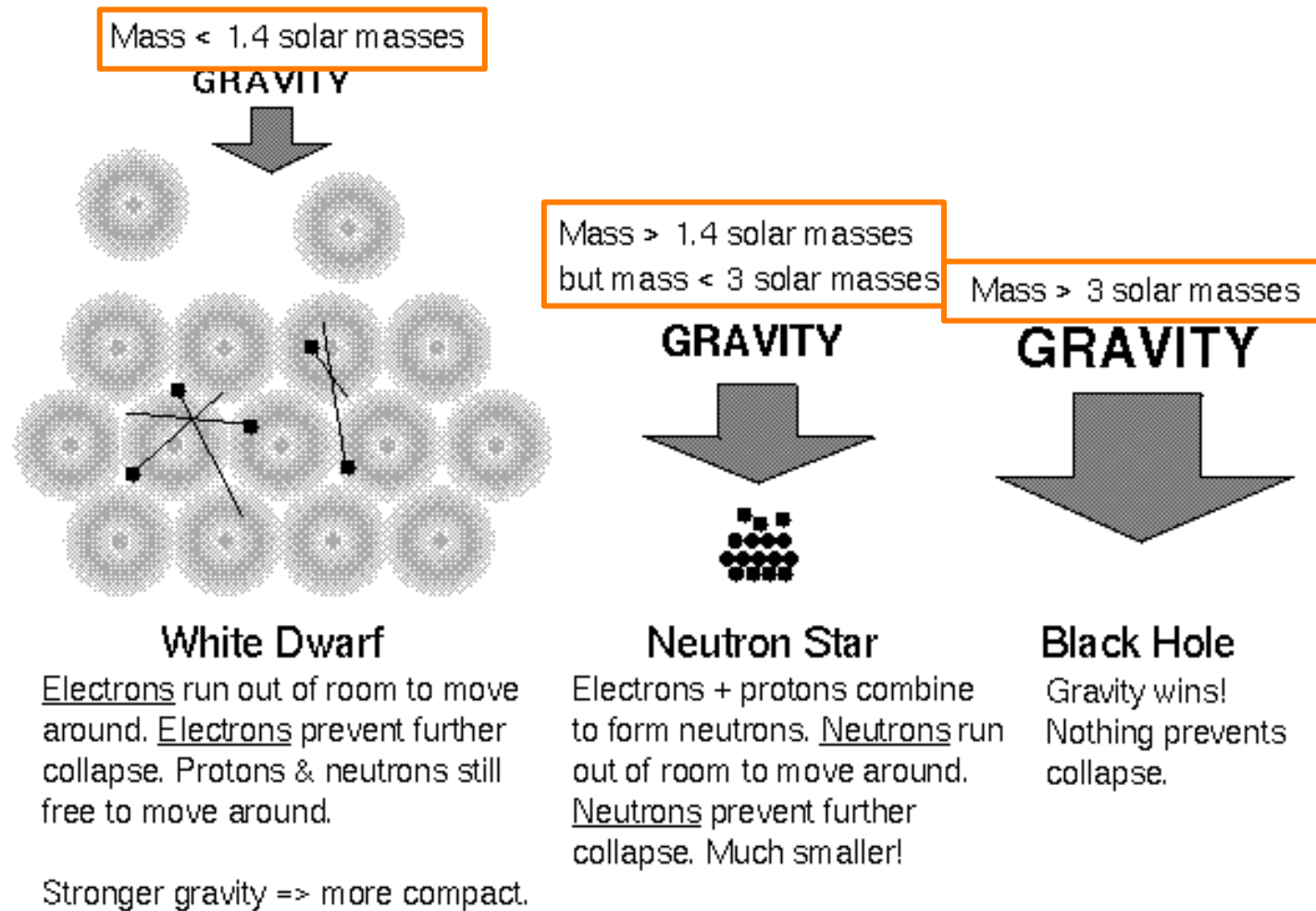
A degenerate star which is supported by:

- *electron degeneracy* pressure is called a **white dwarf**
- *neutron degeneracy* pressure is called a **neutron star**

If the remnant core is so massive that the force of gravity is greater than neutron degeneracy pressure...

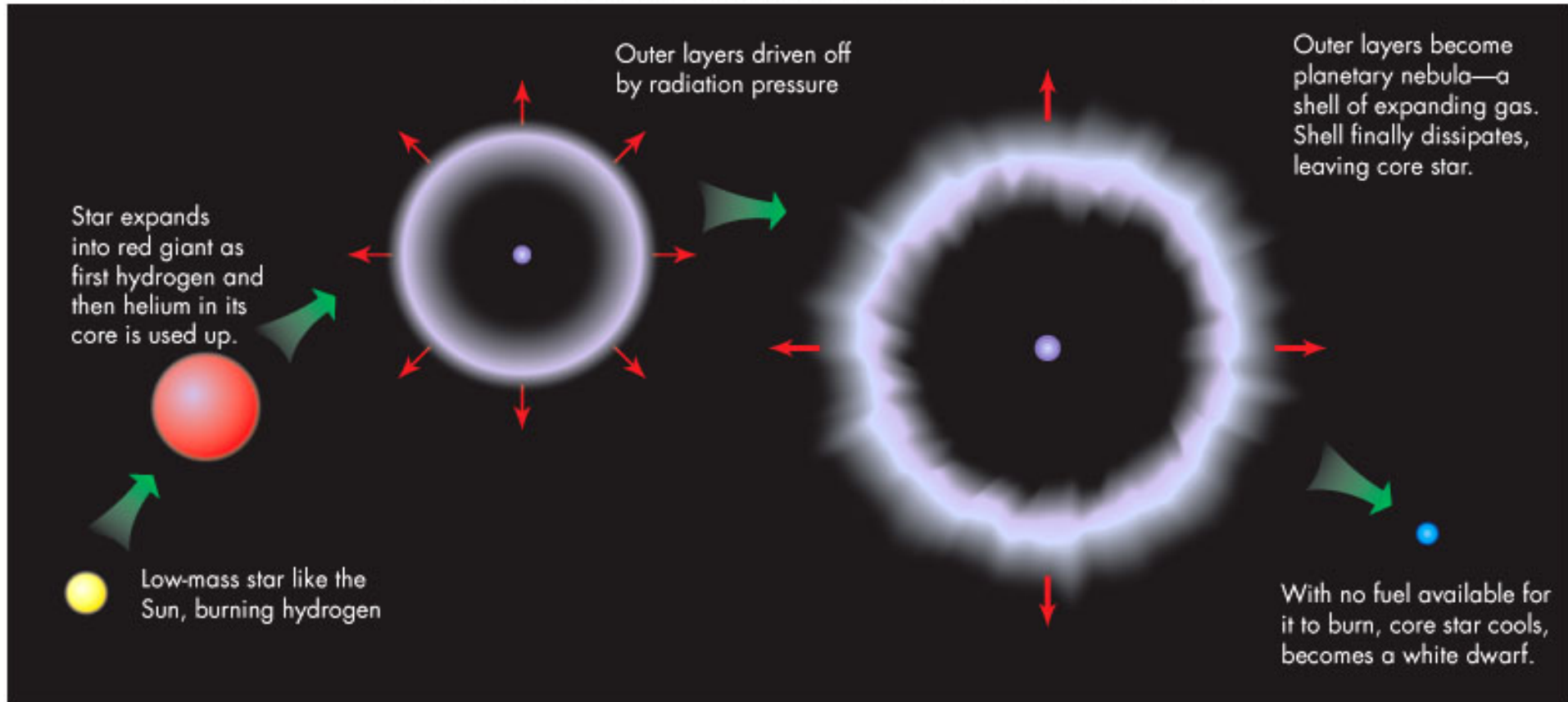
- the star collapses out of existence and is called a **black hole**

# The bizarre stellar graveyard

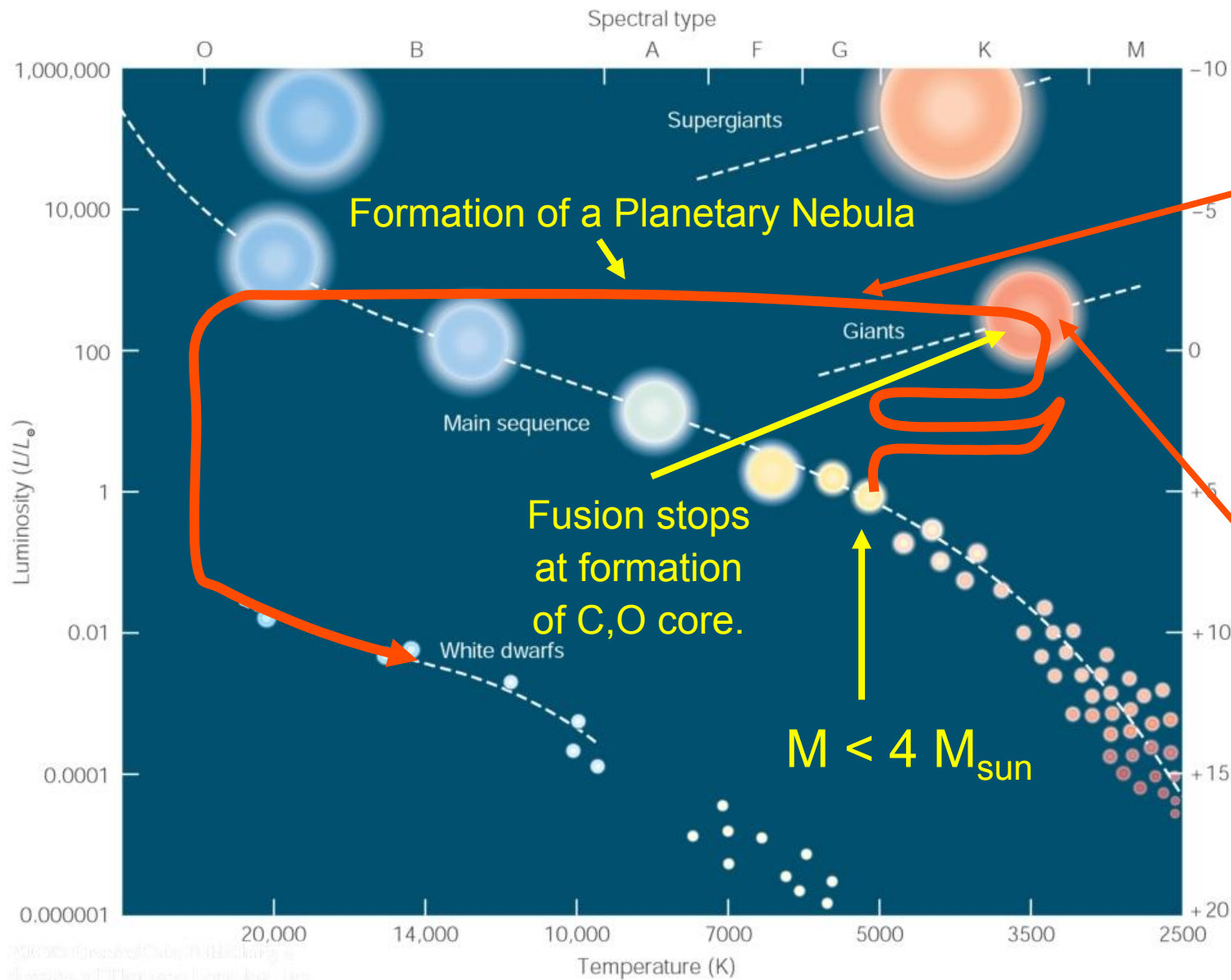


# White dwarfs in stellar evolution

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$M < 8M_{\odot}$ : after the red giant phase, the star gets rid of its outer layers becoming a planetary nebula. When the shell dissipates, only the core star (white dwarf), with a degenerate nucleus, is left



Core collapses;  
outer shells  
bounce off the  
hard surface of  
the degenerate  
C,O core

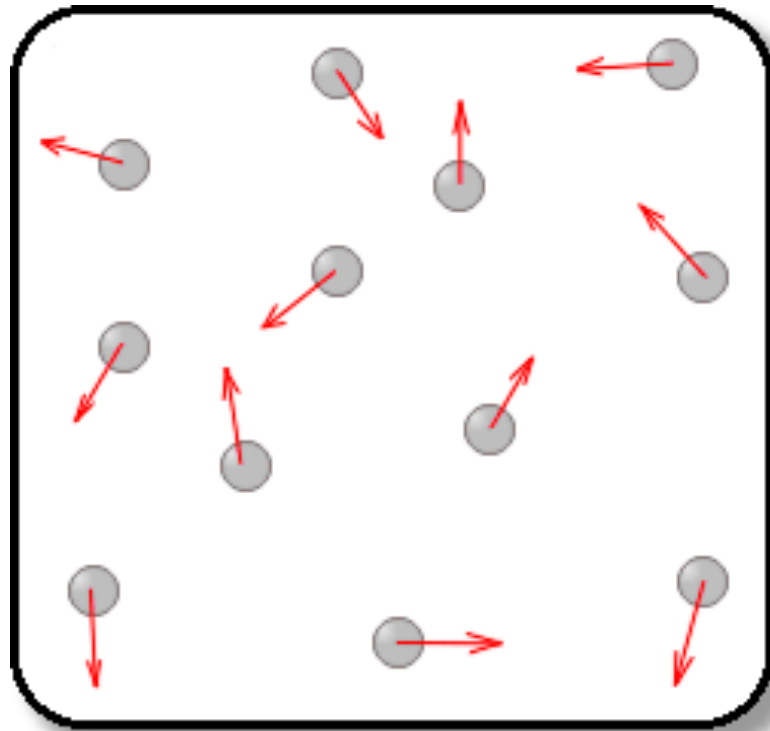
C,O core  
becomes  
degenerate

## White dwarf: main properties

- 1.4 Solar masses (Chandrasekhar limit) and below
- After a Red Giant has shed its planetary nebula, if a mass of 1.4 times that of our Sun or lower remains, the star collapses due to gravity and becomes a white dwarf
- A  $1.4 M_{\odot}$  star can exert an outward pressure equal to the inward force of gravity. The pressure comes from Electron Degeneracy
- The more massive a White dwarf the smaller its radius
- A White Dwarf just at this mass has the highest density and the smallest radius possible for electron degeneracy to keep it stable. More mass and the star will gravitationally collapse further
- The high surface gravity causes lighter elements to be separated by heavier elements → observed H-dominated and He-dominated spectra

## Normal gas

- Pressure is the force exerted by atoms in a gas
- Temperature is how fast atoms in a gas move

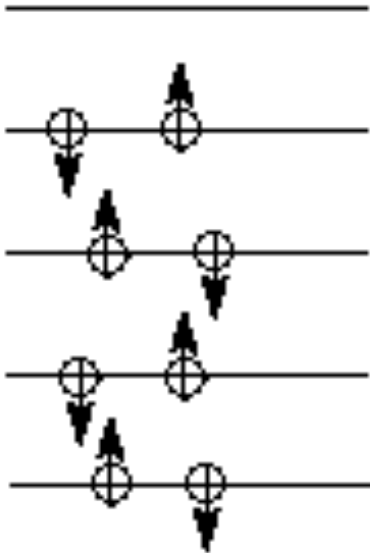


- Hotter → atoms move faster → higher pressure
- Cooler → atoms move slower → lower pressure

$$PV = NkT$$



# Electron energy level



**Degenerate** gas: all lower energy levels filled with two particles each (opposite spins). Particles **locked** in place.

- Only two electrons (one up, one down) can go into each energy level (*Pauli Exclusion Principle*).
- In a *degenerate gas*, all low-energy levels are filled according to Pauli principle.
- Electrons have energy, and therefore are in motion and exert pressure even if temperature is zero.
- White dwarfs are supported by electron degeneracy.

# Electron degeneracy pressure

*Pauli Exclusion principle* – two particles cannot be in the same quantum state (i.e. quantum numbers that describe energy level, spin must differ).

*Degenerate gas* - compressed/cooled gas such that all electrons are in lowest energy levels allowed by exclusion principle

*Heisenberg Uncertainty principle* -  $\Delta p \Delta x \geq h/2\pi$

Since particle's location ( $\Delta x$ ) is extremely confined, momentum ( $\Delta p$ ) is very uncertain and particles are moving extremely fast  $\rightarrow$  this leads to high pressure for a degenerate gas.

$$P = 2(h/2\pi)^2 (Z/A)^{5/3} (\rho/m_p)^{5/3} /m_e$$

A is the atomic mass number, Z is the charge number (# of  $e^-$  carried by each ion)

Chandrasekhar found the maximum pressure exerted by a degenerate electron gas with  $v = c$  allowing for special relativistic effects. This pressure corresponds to a maximum mass of  $1.44 M_\odot$ .

## Some calculations (I)

$$\Delta x \Delta p \approx \hbar$$

Heisenberg's uncertainty principle

$\Delta x$ =distance between electrons  $\approx 1/n_e^{1/3}$

$\Delta p$ =uncertainty on the momentum of the particles

$n_e$ =number of electron per unit volume

$N_e$ =total number of electrons available

$$p \approx \Delta p \approx \hbar / \Delta x \approx \hbar n_e^{1/3}$$

Momentum of an electron

$$E \approx \frac{1}{2} m_e v^2 = \frac{p^2}{2m_e} \approx \frac{\hbar^2 n_e^{2/3}}{2m_e}$$

Energy of a typical electron ( $\approx$ Fermi energy)

$$E_{tot,deg} \approx N_e E = \frac{N_e \hbar^2 n_e^{2/3}}{2m_e}$$

Total degeneracy energy

## Some calculations (II)

$$N_e = M \frac{Z}{Am_p} = \frac{M\beta}{m_p}$$

$$n_e = \frac{N_e}{V} \approx \frac{N_e}{R^3}$$

M=Mass of the star

Z=number of electrons per atom

A=atomic mass (number of nucleons per atom)

R=radius of the star

$\beta=Z/A$

$$E_{tot} = \frac{N_e \hbar^2 n_e^{2/3}}{2m_e} = \frac{N_e^{5/3} \hbar^2}{2m_e R^2} = \frac{\hbar^2 \beta^{5/3}}{2m_e m_p^{5/3}} M^{5/3} R^{-2}$$

$$\text{Equilibrium: } E_{\text{tot,deg}} = E_{\text{gr}} = GM^2/R$$

$$\frac{\hbar^2 \beta^{5/3}}{2m_e m_p^{5/3}} M^{5/3} R^{-2} = \frac{GM^2}{R} \rightarrow R = \frac{\hbar^2 \beta^{5/3}}{2Gm_e m_p^{5/3}} M^{-1/3}$$

$$\Rightarrow R \propto M^{-1/3}$$

## Some calculations (III)

$$R \approx 2 \times 10^4 \left( \frac{\beta}{0.5} \right)^{5/3} \left( \frac{M}{M_{sun}} \right)^{-1/3} \text{ km}$$

Not-relativistic case


$$P = \frac{n_e}{m_e} p^2 \propto \rho^{5/3}$$

Pressure depends only on density [ $\neq f(T, \rho)$ ]

$$E \approx pc \approx \hbar n_e^{1/3} c$$

Relativistic case

$$E_{tot,deg} = N_e E \approx \frac{\hbar \beta^{4/3} c}{m_p^{4/3}} M^{4/3} R^{-1}$$

 
$$M_{Ch} \approx \left( \frac{\hbar \beta^{4/3} c}{G m_p^{4/3}} \right)^{3/2} \approx 5.9 \beta^2 M_{sun}$$

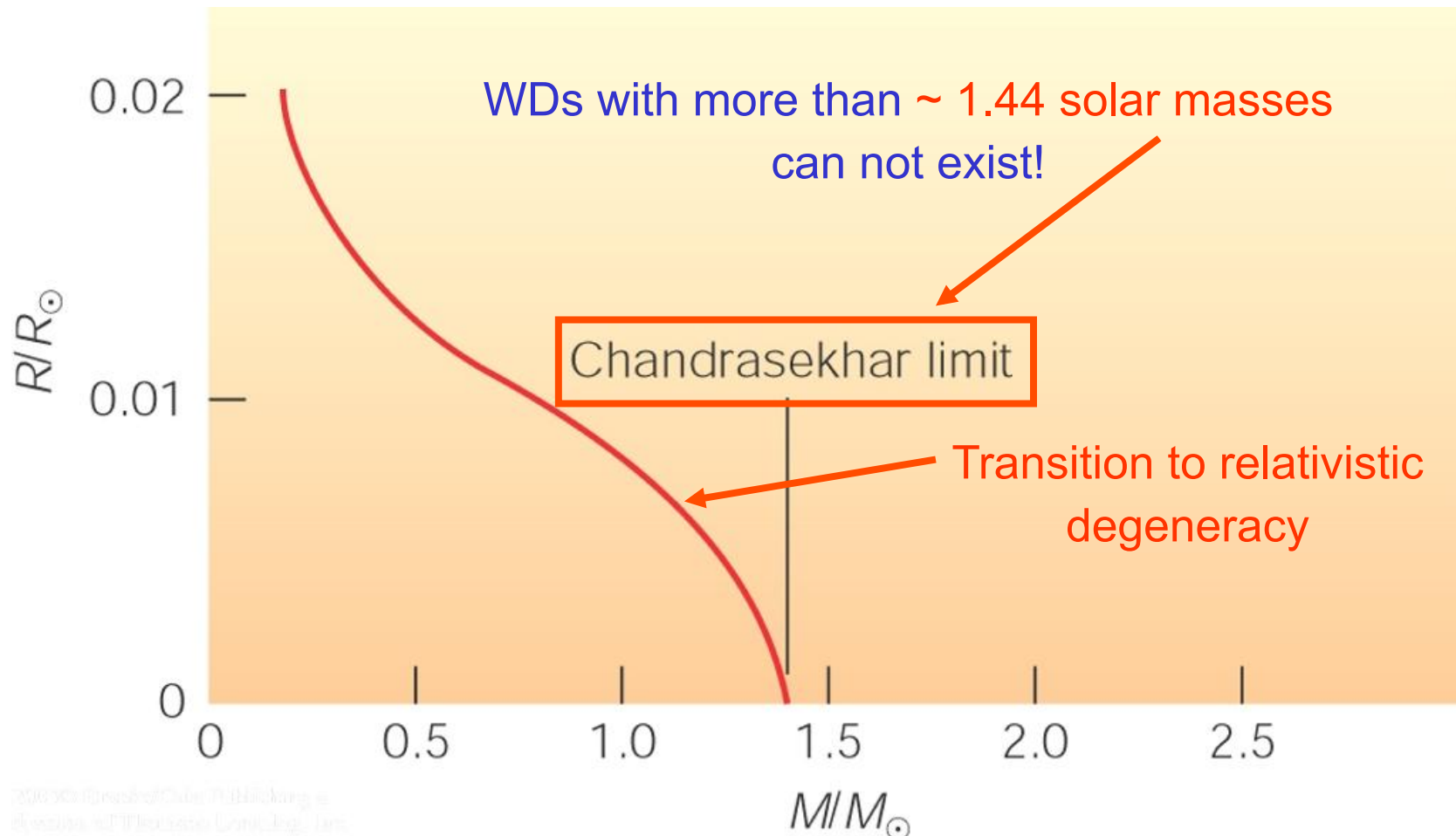
$$P \approx 0.8 \hbar c \beta^{4/3} \left( \frac{\rho}{m_p} \right)^{4/3} \propto \rho^{4/3}$$

Chandrasekhar mass (limit for a WD)  $\approx 1.4 M_{\odot} \rightarrow$  gravity overcomes the resistance of  $P_{deg}$ . The resulting collapse raises  $T \rightarrow$  C+O in the core starts to fuse  $\rightarrow$  explosive wave propagating through the core rapidly  $\rightarrow$  solar mass of radioactive  $^{56}\text{Ni}$  and  $\sim 10^{52}$  erg release of energy, disrupting the ★

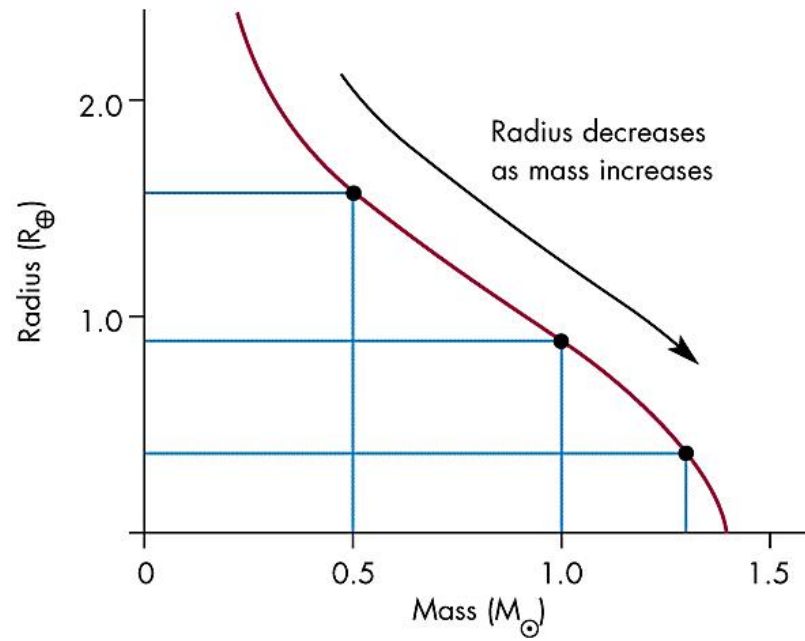
# The Chandrasekhar limit

The more massive a white dwarf, the smaller it is.

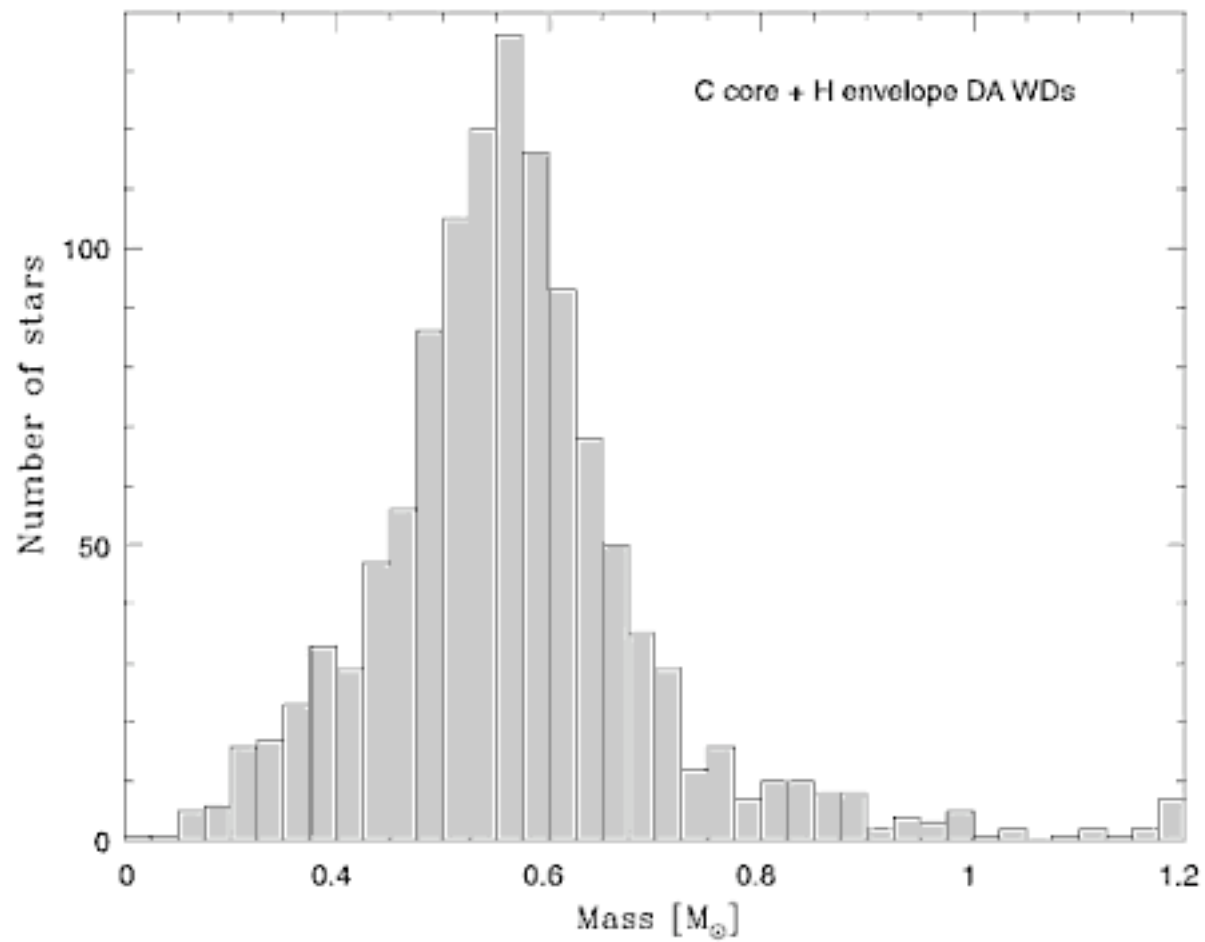
$$R_{\text{WD}} \sim M_{\text{WD}}^{-1/3} \Rightarrow M_{\text{WD}} V_{\text{WD}} = \text{const. (non-rel.)}$$



# Mass vs. radius relation



# Mass distribution

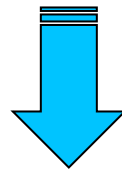
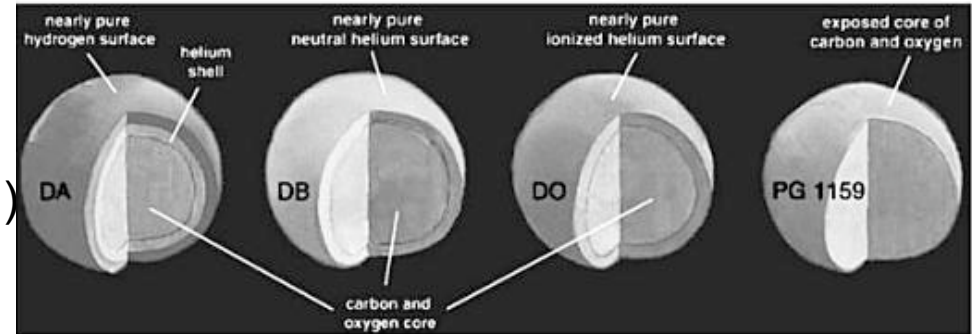




# **White dwarf: classification**

# Surface compositions

- DA: strong H lines ( $\approx 80\%$  pop.)
- DB: strong He I lines ( $\approx 15\%$  pop.)
- DO: strong He II lines
- DC: no strong lines (continuous spectrum)
- DZ: strong metal lines (excluding C)
- DW: strong C lines



DA  
not-DA

– H-rich, H Balmer lines, normal stellar evolution

– H-poor, He lines → late He-shell flash in the early cooling phase

→ re-traces the post-AGB evolution

→ H burns again + convective mixing

→ He, C, and O-rich materials dredged up to the surface

typically very hot

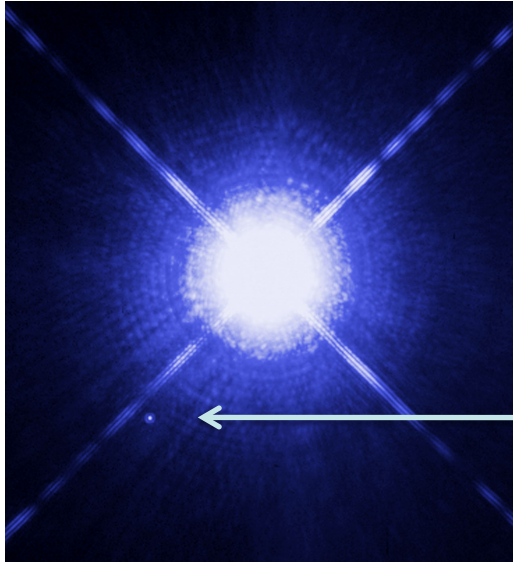
DA: wide range of T (lower envelope of DO temperatures)

DO:  $T \approx 45000 - 120000$  K (HeII)

DB:  $T \approx 12000 - 30000$  K (HeI)

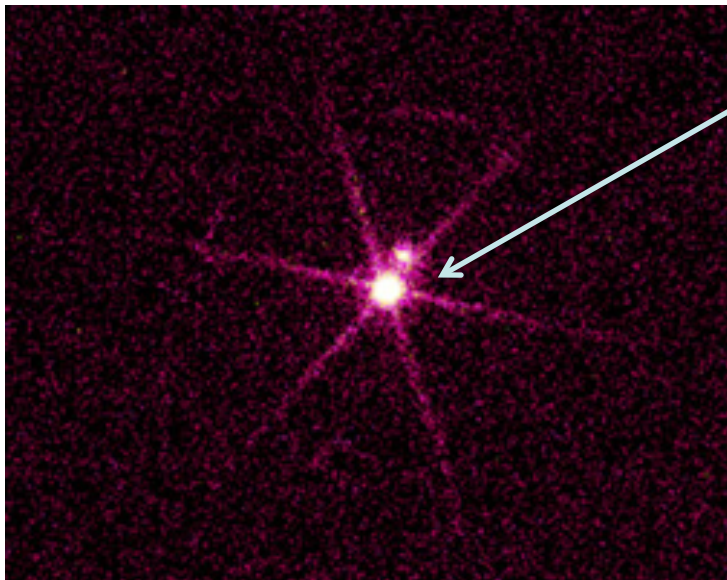
DC:  $T < 12000$  K

# White dwarfs in X-rays



First example:

*Sirius B* - discovered  
in 1862



$$M \approx 1 M_{\odot}$$

$$L \approx 0.03 L_{\odot}$$

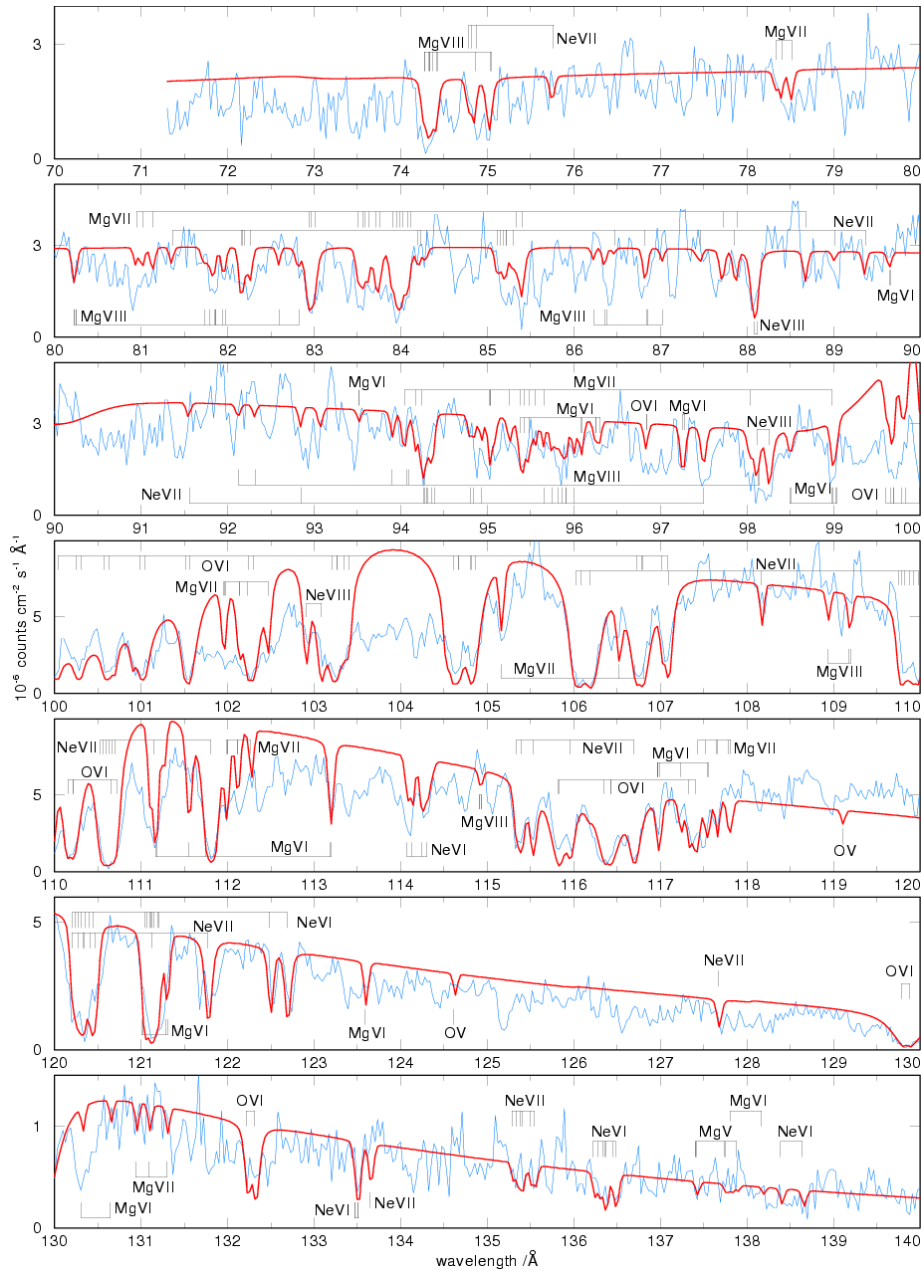
$$T_e \approx 27,000 \text{ K}$$

$$\Rightarrow R \approx 0.008 R_{\odot}$$

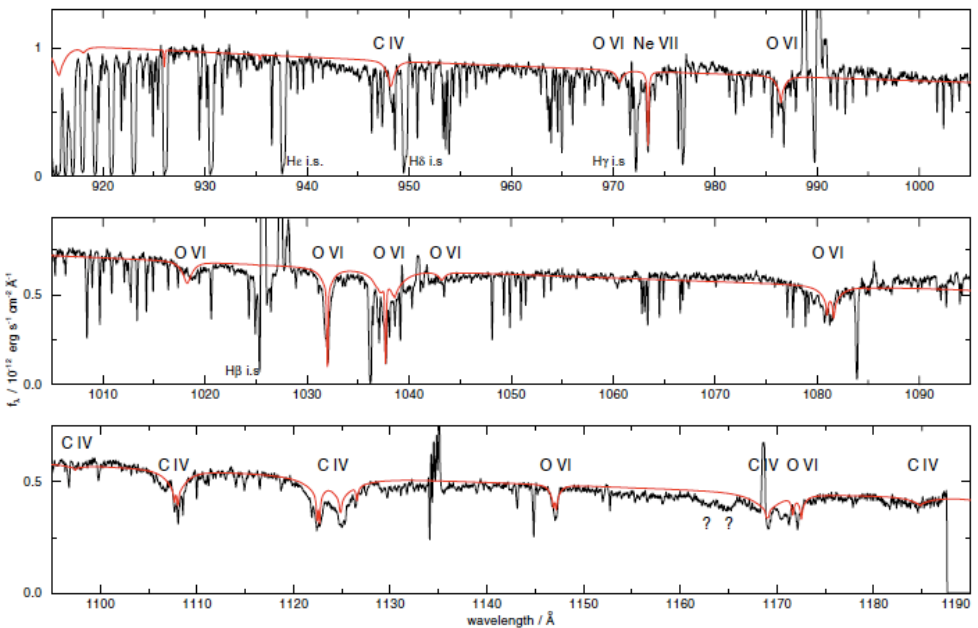
$$\Rightarrow \rho \approx 3 \times 10^6 \text{ g/cm}^3$$

## What causes the UV and soft X-ray emission

- *High-energy photons in the deep and hot inner layers of the star* are responsible for the emission, well parameterized by pure H models for atmospheres. The low opacity of the atmosphere allows soft X-ray emission to be detected
- At  $T_{\text{eff}} < 40,000$ , these models predict an X-ray flux which is often much larger than that measured
- Original surveys with *ROSAT* (RASS) predicted more X-ray bright WDs than actually discovered
- ➔ Indications of the presence of metals in the atmosphere, increasing the opacity to X-ray photons, but strong ionization reduces the opacity in the soft X-ray band
- X-ray emission is expected to be soft, but some (<10) WDs are hard X-ray emitters (50% of which are among the hottest WDs) ➔ thermal origin from very deep photospheric layers?
- PG1159 star-class: non-DA progenitors,  $T > 140,000\text{K}$ : high C+O abundance and He in their photospheres. Hot enough to suppress He II opacity



$\lambda(\text{\AA})$



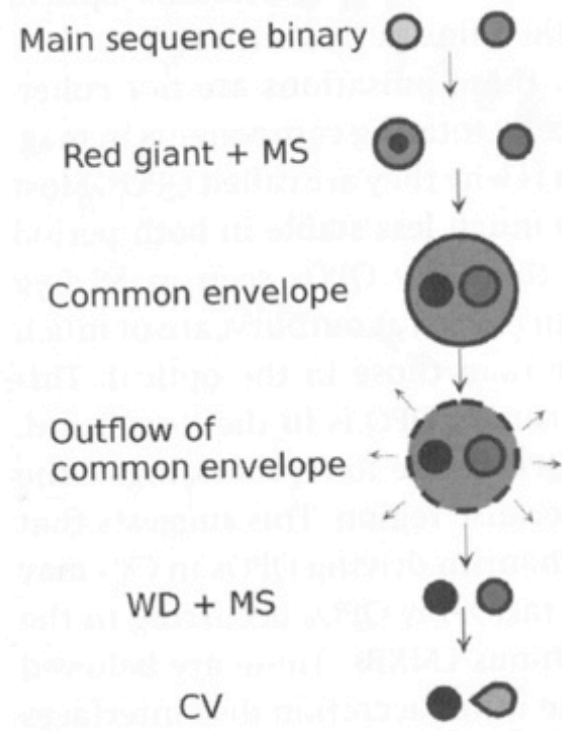
H1504+65: *Chandra* and *FUSE*  
 high-resolution spectra + model (red line)  
 Naked CO WD or WD with O-Ne-Mg core  
 after C burning?  
 $T_{\text{eff}} \approx 200,000\text{K}$  (highest T measured)

Good models required to account for  
 vertical stratification of chemical  
 abundances

# **White dwarf in binary systems**

From main-sequence stars to a CV

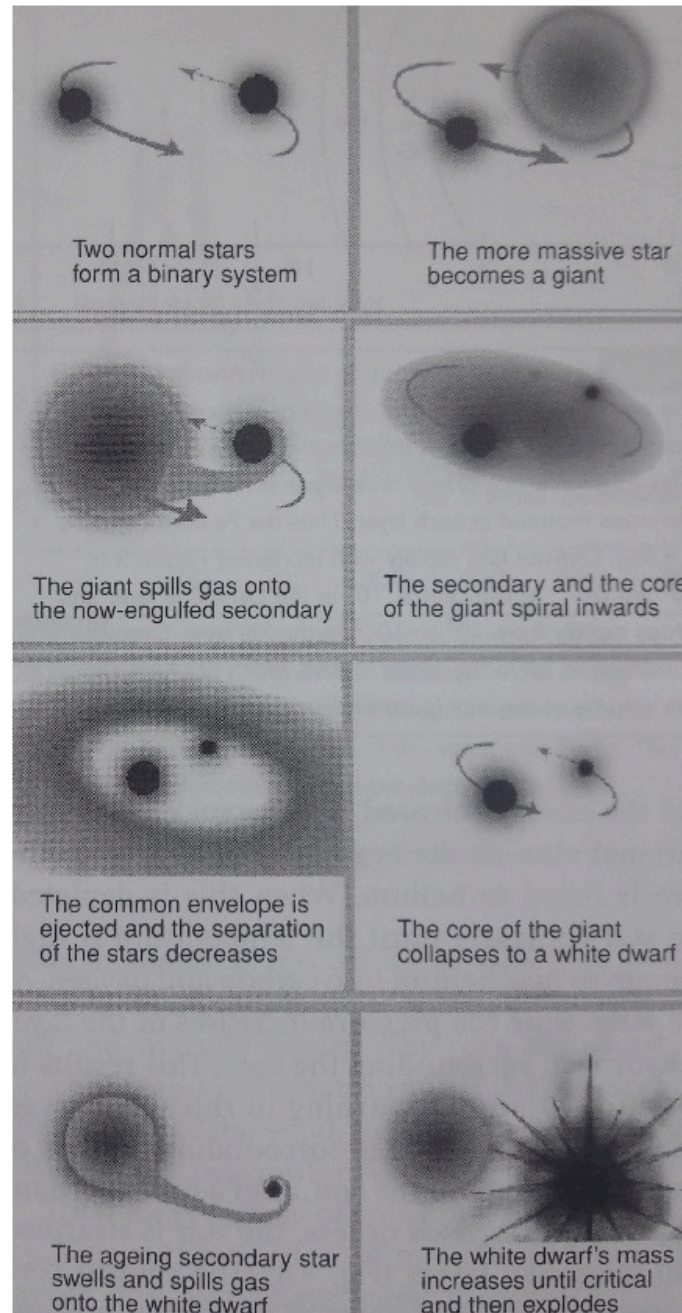
Interacting binary evolution



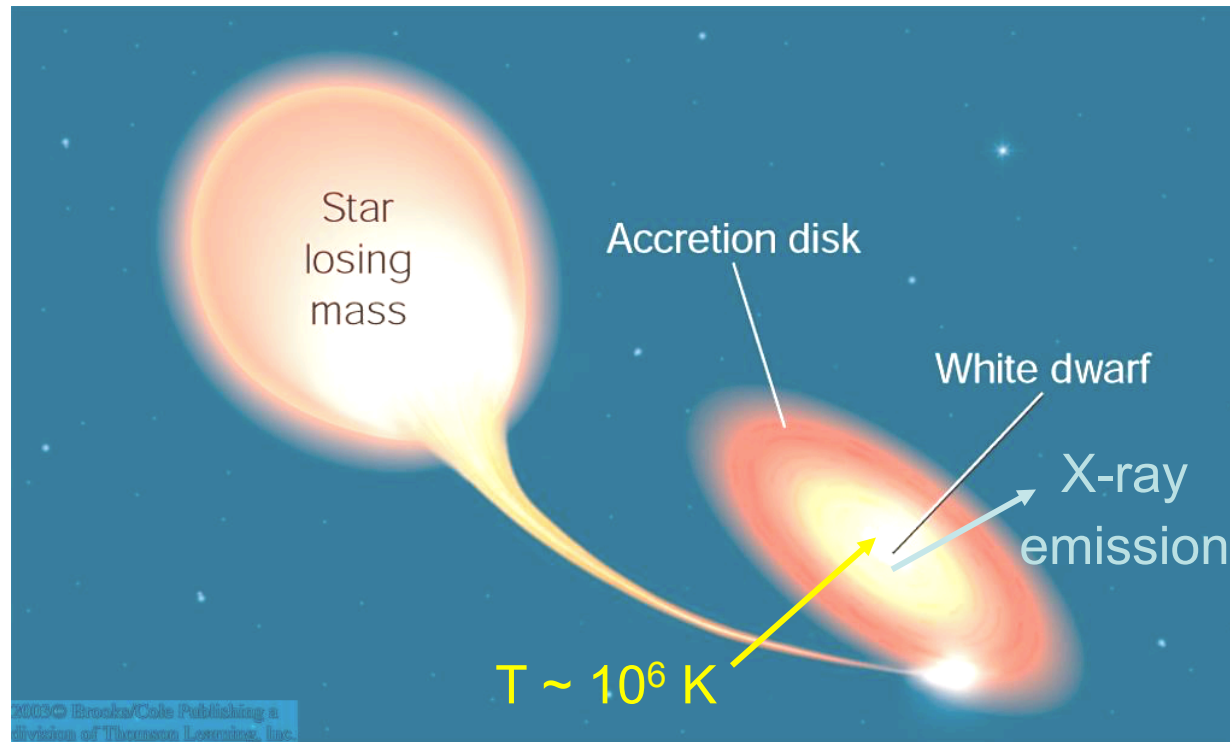
Double stars are easily produced in large star-forming regions (e.g., the Orion Nebula), with wide separations and orbital periods of years. The most massive star of the system will evolve more rapidly and start expanding into a red giant; its atmosphere will embrace the other star, which will then spiral in towards the core of the red giant (because of atmospheric drag) → common tenuous envelope. Eventually the companion star will evolve and fill its own Roche lobe → mass transfer onto the WD.



From a binary star system  
to a WD explosion



# White dwarfs in binary systems



Binary consisting of WD + MS or Red Giant star → WD accretes matter from the outer layers of the companion star

Angular momentum conservation => accreted matter forms a disk, called **accretion disk**.

Matter in the accretion disk heats up to ~ 1 million K  
→ X-ray emission → "X-ray binary".