#### The Galactic Center

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with slides from R. Genzel, S. Gillessen, and the MPE GC group mpe.mpg.de/ir/GC

ESO/Y. Beletsky

#### The Galactic Center

1. Seminar: strong gravity around Sgr A\* (30.05)

2. Low-luminosity accretion onto Sgr A\* (today)
i. Why is Sgr A\* so faint? (accretion theory)
ii. Sgr A\* IR / X-ray flares

3. Resolving the event horizon of a black hole with interferometry (01.06)

#### About the lectures

Selected topics: highly biasedPlease ask questions!

~1 interactive Q / lecture:
 ~10 mins to think/calculate, discuss, share

#### About the lectures

 pdf of slides online: mpe.mpg.de/~jdexter/GCslides

 Further reading: Genzel+2010, Morris+2012, Falcke & Markoff 2013

#### The Galactic Center

### 2. Low-luminosity accretion theory (why is Sgr A\* so faint?)

#### Accretion power

Infalling gas radiates its gravitational energy



# Eddington Luminosity

• How bright can accretion be?



$$F_{g} = F_{rad}$$

$$GMm_{p}/r^{2} = L / 4\pi r^{2} \sigma_{T} / c$$

$$L_{edd} = 4\pi Gm_{p} c M / \sigma_{T}$$

$$\sim 10^{38} \text{ ergs / s (M/M_{sun})}$$

Sgr A\*:  $L_{edd} \sim 10^{45}$  ergs / s  $L_{bol} < 10^{37}$  ergs / s

#### Eddington accretion rate

• What is minimum amount of infalling material to get L?



Maximum L: L = dE/dt = d/dt(mc2) $L = Mdot c^2$ 

General L: L =  $\epsilon$  Mdot c<sup>2</sup>

 $\epsilon$  = "accretion efficiency"

#### Large gas reservoirs in the GC

#### Stellar winds: black hole fuel

Mdot ~ 10<sup>-4</sup> – 10<sup>-3</sup> Msun / yr (Martins+2007)



Cuadra +2006, 2008

#### X-rays from Sgr A\*



# X-rays from Sgr A\*



#### **Bondi-Hoyle** accretion

• Mdot =  $4\pi\rho G^2 M^2 / (v^2 + c_s^2)^{3/2}$ 



#### **Bondi-Hoyle** accretion

- Mdot =  $4\pi\rho G^2 M^2 / (v^2 + c_s^2)^{3/2}$
- X-rays:
   n ~ 100 cm<sup>-3</sup>,
   T ~ 10<sup>7</sup> K
- Winds: v ~ 1000 km / s
- Mdot ~ 10<sup>-5</sup> M<sub>sun</sub> / yr

#### Quataert+1999, 2004



# Q: Why is it difficult for gas to fall into a black hole?

- Sgr A\* Bondi radius R ~ 0.1 pc: what is the angular momentum of a circular orbit?
- What fraction of this must be lost to reach the event horizon, R ~ 10<sup>-6</sup> pc?
- Or: what eccentricity is needed for orbit from Bondi radius to reach event horizon?

- Hydrodynamics equations (collisional, viscous fluid)
- Stationary, axisymmetric ( $d_t = d_{\phi} = 0$ )
- Vertically integrate over z (H/R < 1)
- Parameters: Mdot = constant, H/R < 1, alpha</li>



- Mass flux = const. =  $\rho v A$
- $A = 2\pi R 2H$

#### $\dot{\mathbf{M}} = 4\pi \mathbf{R} \mathbf{H} ho \mathbf{v}$



 Stress transports angular momentum

G(R)= $\tau A$ , L(R)=R<sup>2</sup> $\Omega$ 

Mdot  $dL/dR = -dG/dR^{1}$ 



- Stress transports angular momentum
- What is τ?

$$egin{aligned} & au_{\mathbf{r}\phi} = 
ho 
u \mathbf{R} rac{\mathbf{d} \mathbf{\Omega}}{\mathbf{d} \mathbf{R}} \ & = lpha \mathbf{P} rac{\mathbf{R}}{\mathbf{\Omega}_{\mathbf{K}}} rac{\mathbf{d} \mathbf{\Omega}}{\mathbf{d} \mathbf{R}} \end{aligned}$$



- Stress transports angular momentum
- What is τ?

$$\tau_{\mathbf{r}\phi} = \rho \nu \mathbf{R} \frac{\mathbf{d}\Omega}{\mathbf{d}\mathbf{R}}$$
$$= \alpha \mathbf{P} \frac{\mathbf{R}}{\mathbf{\Omega}_{\mathbf{K}}} \frac{\mathbf{d}\Omega}{\mathbf{d}\mathbf{R}}$$
"\alpha model"

Shakura & Sunyaev 1973



• Mass:

Shakura & Sunyaev 1973, here following Blaes 2004

$$\mathbf{M} = \mathbf{4}\pi\mathbf{R}\mathbf{H}
ho\mathbf{v}$$

- Momentum:  $\rho \mathbf{v} \, \mathbf{d_R v} = \rho (\mathbf{\Omega^2} \mathbf{\Omega_K^2}) \mathbf{R} \mathbf{d_R p}$
- Angular momentum:  $\dot{\mathbf{M}} \mathbf{d}_{\mathbf{R}}(\mathbf{\Omega}\mathbf{R}^2) = \mathbf{d}_{\mathbf{R}}(4\pi \mathbf{R}^2 \mathbf{H} \tau_{\mathrm{R}\phi})$
- Energy:  $\frac{\dot{\mathbf{M}}}{2\pi\rho\mathbf{R}}\mathbf{T}\,\mathbf{d_R}\mathbf{s} = \mathbf{Q}^+$  -  $\mathbf{Q}^ \frac{\dot{\mathbf{M}}}{2\pi\rho\mathbf{R}}\mathbf{T}\,\mathbf{d_R}\mathbf{s} = \mathbf{2}\mathbf{R}\mathbf{H}\tau_{\mathrm{R}\phi}\,\mathbf{d_R}\mathbf{\Omega} + \mathbf{2}\mathbf{F}^-$

- Ω = Ω<sub>K</sub>, Mdot = constant, Q<sup>+</sup> = Q<sup>-</sup> (Q<sup>adv</sup> = 0), no torque at inner edge (R<sub>i</sub>)
- Angular momentum:

$$\begin{split} \dot{\mathbf{M}} \, \mathbf{d}_{\mathbf{R}}(\mathbf{\Omega}\mathbf{R}^2) &= \mathbf{d}_{\mathbf{R}}(4\pi\mathbf{R}^2\mathbf{H}\tau_{\mathbf{R}\phi}) \\ \dot{\mathbf{M}}(\mathbf{\Omega}_{\mathbf{K}}\mathbf{R}^2 - \mathbf{\Omega}_{\mathbf{K},\mathbf{i}}\mathbf{R}_{\mathbf{i}}^2) &= 4\pi\mathbf{H}\mathbf{R}^2\tau_{\mathbf{R}\phi} \end{split}$$

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• Energy:

 $rac{\dot{\mathbf{M}}}{2\pi
ho\mathbf{R}}\mathbf{T}\,\mathbf{d_Rs}=\mathbf{2RH} au_{\mathrm{R}\phi}\,\mathbf{d_R}\mathbf{\Omega}+\mathbf{2F}^-$ 

 $\mathbf{F}^{-}=-\mathbf{R}\mathbf{H} au_{\mathbf{R}\phi}\mathbf{d}_{\mathbf{R}}\mathbf{\Omega}_{\mathbf{K}}$ 

# Thin disk accretion Solve for flux emerging from disk, F<sup>-</sup>

# $\dot{\mathbf{M}}(\mathbf{\Omega}_{\mathbf{K}}\mathbf{R}^{2} - \mathbf{\Omega}_{\mathbf{K},\mathbf{i}}\mathbf{R}_{\mathbf{i}}^{2}) = 4\pi\mathbf{H}\mathbf{R}^{2}\tau_{\mathbf{R}\phi}$

#### $\mathbf{F}^{-}=-\mathbf{R}\mathbf{H} au_{\mathbf{R}\phi}\mathbf{d}_{\mathbf{R}}\mathbf{\Omega}_{\mathbf{K}}$

# Thin disk accretion Solve for flux emerging from disk, F<sup>-</sup>

 $\dot{\mathbf{M}}(\boldsymbol{\Omega_{\mathbf{K}}R^2} - \boldsymbol{\Omega_{\mathbf{K},i}R_i^2}) = 4\pi \mathbf{HR^2} \tau_{\mathbf{R}\phi}$ 

 $\mathbf{F}^{-}=-\mathbf{R}\mathbf{H} au_{\mathbf{R}\phi}\mathbf{d}_{\mathbf{R}}\mathbf{\Omega}_{\mathbf{K}}$ 

•  $\Omega_{\rm K}^{2} = {\rm GM}/{\rm R}^{3}$ ,  ${\rm d}_{\rm R}\Omega_{\rm K}^{2} = -3/2 \ \Omega_{\rm K}^{2} / {\rm R}$ :

$$egin{aligned} \mathbf{F}^-(\mathbf{r}) &= rac{3 \mathbf{GM} \dot{\mathbf{M}}}{8 \pi \mathbf{R}^3} \left( \mathbf{1} - \sqrt{rac{\mathbf{R}_{ ext{in}}}{\mathbf{R}}} 
ight) \ \mathbf{L} &= \mathbf{2} \int_{\mathbf{R}_{ ext{i}}}^\infty \mathbf{d} \mathbf{R} \, \mathbf{2} \pi \mathbf{R} \, \mathbf{F}^-(\mathbf{R}) \end{aligned}$$

• Solve for total luminosity integrated over disk:

$$egin{aligned} \mathbf{L} &= 2 \int_{\mathbf{R}_{i}}^{\infty} \mathbf{d} \mathbf{R} \, 2\pi \mathbf{R} \, \mathbf{F}^{-}(\mathbf{R}) \ \mathbf{L} &= \dot{\mathbf{G}} \mathbf{M} \dot{\mathbf{M}} \ \mathbf{L} &= \frac{\mathbf{G} \mathbf{M} \dot{\mathbf{M}}}{2\mathbf{R}_{i}} \end{aligned}$$

• Solve for total luminosity integrated over disk:

$$\begin{split} \mathbf{L} &= 2 \int_{\mathbf{R}_{i}}^{\infty} \mathbf{d}\mathbf{R} \, 2\pi \mathbf{R} \, \mathbf{F}^{-}(\mathbf{R}) \\ \mathbf{L} &= \frac{\mathbf{G}\mathbf{M}\mathbf{\dot{M}}}{\mathbf{2}\mathbf{R}_{i}} \end{split}$$

- $R_i \sim \text{innermost stable circular orbit of a}$ black hole = 6 GM/c<sup>2</sup> = 6  $r_g$  = for spin zero
- L ~ 10% Mdot c<sup>2</sup>!
- Compare: nuclear fusion ~ 0.1% Mdot c<sup>2</sup>

- opt. thick, so  $L = 4\pi R^2 \sigma T_{eff}^4$
- R ~ M, mdot = Mdot  $c^2 / L_{edd}$
- T<sub>eff</sub> ~ mdot<sup>1/4</sup> M<sup>-1/4</sup>
- Stellar black holes in X-rays, AGN in UV



#### Sgr A\* SED



v [Hz]

# Thin disks don't work for Sgr A\*

- Thin disk:
   L ~ 10<sup>5</sup> too bright;
   spectrum should peak
   in IR not submm
- If Mdot ~ Mdot<sub>Bondi</sub>,  $\epsilon = L / Mdot c^2 ~ 10^{-5}!$
- Why is Sgr A\* so faint?



 Thin disk assumes rapid cooling. Breaks down when cooling time becomes long (Rees+1982).

• 
$$t_{cool}/t_{inflow} < 1$$
:

 $t_{cool} = u / \epsilon \sim nkT / n^2\Lambda; \quad t_{inflow} = \Omega^{-1} \alpha^{-1} (H/R)^{-2}$ 

 $t_{cool}/t_{inflow} \sim (kT)^{1/2}/n \ \Omega \alpha$ 

- Vertical hydrostatic equilibrium:  $p/n = kT \sim GMm_p/R^3H \sim m_pc^2 r_g/R (H/R)^2$
- mdot = Mdot/Mdot<sub>Edd</sub> ~ n  $t_{inflow}^{-1}$  (H/R)<sup>-1</sup>

- Vertical hydrostatic equilibrium:  $p/n = kT \sim GMm_p/R^3H \sim m_pc^2 r_g/R (H/R)^2$
- mdot = Mdot/Mdot<sub>Edd</sub> ~ n  $t_{inflow}^{-1}$  (H/R)<sup>-1</sup>

$$t_{cool}/t_{inflow} \sim (kT)^{1/2}/n \Omega \alpha$$
  
 $\Rightarrow t_{cool}/t_{inflow} \sim mdot^{-1} \alpha^{2}$ 

- At small mdot, cooling cannot keep disk thin and solution no longer applies
- Sgr A\*: mdot ~ 10<sup>-6</sup>

 Parameterize fraction of local heating advected (Narayan & Yi 1994): Q<sup>adv</sup> = f Q<sup>+</sup>

- f=0 (Q<sup>-</sup> = Q<sup>+</sup>): cooling,  $\Omega = \Omega_{K}$ , thin disk

- f=1 (Q<sup>adv</sup> = Q<sup>+</sup>): advection,  $\Omega << \Omega_{K}$ , spherical

Self-similar scalings:

 $ho, \mathbf{\Omega} \propto \mathbf{R^{-3/2}}; \ \mathbf{v}, \mathbf{c_s} \propto \mathbf{R^{-1/2}}$ 

• f=1 solutions: v ~ 0.2 v<sub>ff</sub>,  $\Omega$  ~ 0.4  $\Omega_{\rm K}$ , H/R ~ 1




## Observed states as function of mdot

Soft states

Hard states

Sgl



#### **ADAF thermodynamics**

Low density,
 "collisionless," →
 T<sub>e</sub> << T<sub>p</sub>, e- heating is an important open Q

 Plasma effects can be important



# ADAF model of Sgr A\*: low density, hot

- $T_i \sim 10^{12}$  K,  $T_e < 10^{10}$  K,  $n \sim 10^9$  cm<sup>-3</sup>
- e- cannot radiate away heat, energy lost to BH



## Radiation processes in disks

- Bremsstrahlung ~ n<sup>2</sup>
- $a \sim e^2/mb$   $P = \frac{2e^2a^2}{3c^3}$  $P_{br} = \frac{3}{16}\sigma_T c Z U_E$

(not so useful  $b/c U_E$  depends on b)

hν

b

#### Radiation processes in disks

- Synchrotron ~ nB<sup>2</sup>
- $a = e v B \sin \theta / m c$   $P = \frac{2e^2a^2}{3c^3}$ 
  - $U_B = B^2 / 8\pi$  $P_S = \frac{4}{3}\sigma_T c \beta^2 \gamma^2 U_B$



#### Radiation processes in disks

(inverse) Compton scattering ~ n n<sub>ph</sub>



#### Radiation processes in Sgr A\*

- L ~  $10^{36}$  erg / s, R ~  $5 R_{s} = 5 \times 10^{12} cm$ , B ~ 30 G, T<sub>e</sub> ~  $3 \times 10^{10}$  K, n ~  $3 \times 10^{6} cm^{-3}$
- $U_{ph} = 4\pi/c J$
- $U_B = B^2/8\pi$

#### Radiation processes in Sgr A\*

- L ~  $10^{36}$  erg / s, R ~  $5 R_{s} = 5 \times 10^{12} cm$ , B ~ 30 G, T<sub>e</sub> ~  $3 \times 10^{10}$  K, n ~  $3 \times 10^{6} cm^{-3}$
- $U_{ph} = 4\pi/c J \sim 1 erg / cm^3$
- $U_B = B^2/8\pi \sim 40 \text{ erg} / \text{ cm}^3$

$$\rightarrow$$
 P<sub>S</sub> > P<sub>C</sub>

• for thermal:  $P_{Br} \sim n^2 T^{1/2}$ ,  $P_S \sim n B^2 T^2$  $\implies P_{Br} / P_S \sim 10^{-3} \beta \theta_e^{-3/2}$ 

#### Example: relative importance



# Accretion Flow Models of Sgr A\*

- Spherical (Melia 1992)
   ADAF (Narayan+1995)
  - $dM/dt \approx dM/dt_{Bondi}$
  - Lower T<sub>e</sub>, large central density (n ~ r<sup>-3/2</sup>)
- Accretion energy is carried into the black hole!



# Polarization, Faraday rotation, and the Sgr A\* accretion rate

n(r), B(r)

• Magnetic field rotates polarization direction  $\chi(v) \sim v_0 + RM c^2/v^2$  $RM \simeq 2.6 \times 10^{-13} \int dl \cdot B n rad/m^2$ 



# Polarization, Faraday rotation, and the Sgr A\* accretion rate

- RM ~ M<sup>-2</sup> Mdot<sup>3/2</sup> (Marrone et al. 2006)
  - $\dot{M} \simeq 10^{-9} r_{
    m NR}^{7/6} M_{\odot} {
    m yr}^{-1}$ r ~ 1-100 R<sub>s</sub>
- > 99% of the mass doesn't accrete!

(Aiken+2000, Agol 2000, Quataert & Gruzinov 2000, Bower+2003, Marrone+2006,2007)



#### Sgr A\* e- temperature

- For known flux, angular size "brightness" temperature is  $B_v(T_b) = I_v$
- Sgr A\* at 230 GHz:  $\mathbf{T_b} = \frac{\mathbf{c^2} \mathbf{I}_\nu}{2 \mathbf{k} \nu^2}$  $\simeq 6 \times 10^{10} \mathrm{K}$ cf.  $T_i \approx T_{vir} \approx 10^{12} \text{ K}$ • Lower limit to T<sub>e</sub>,  $>> 10^9$  K in ADAF
- n ~ 3x10<sup>6</sup> cm<sup>-3</sup>, B ~ 50 G



# Accretion flow models of Sgr A\*

- Outflows → ADIOS (Blandford & Begelman 1999)
- Convection → CDAF (Quataert & Gruzinov 2000)
- ADAF/CDAF/ADIOS/
   ... → "RIAF"
  - Mass loss
  - Non-thermal e- or jet for polarization



## How does gas fall into a black hole?

 Weakly magnetized gas: field is dragged along, restoring force when stretched (torque!)



The MRI can cause accretion Instability  $\rightarrow$  turbulence, stresses  $\rightarrow$  torque

- Stress tensor:
- $T_{r\phi} = -B_r B_{\phi}/4\pi + \rho v_r v_{\phi}$
- Simulations:
  - Maxwell stress is larger
  - $-\alpha \sim -B_r B_{\phi}/4\pi P \sim 0.01-0.1$



Balbus & Hawley 1998 52

#### The MRI can cause accretion Instability $\rightarrow$ turbulence, stresses $\rightarrow$ torque



McKinney & Blandford 2009

# MHD simulations of BH accretion

- Good: physical theory of accretion!
- Bad: turbulence, magnetic fields, timedependence, 3D → numerical simulations
- Work in progress: plasma physics

Sgr A\* is a great laboratory for MRI accretion theory

# Why is Sgr A\* so faint?

	Radius (Rs or pc)	Accretion rate (M <sub>sun</sub> / yr)	Accretion efficiency
Giant molecular clouds	10-100 pc	10-2	10 <sup>-8</sup>
Circumnuclear disk	1-7 pc	10 <sup>-3</sup>	10 <sup>-7</sup>
Winds from massive stars	< 0.5 pc ~ 10 <sup>6</sup> R <sub>s</sub>	10-4 - 10-3	10 <sup>-6</sup> – 10 <sup>-7</sup>
Winds at Bondi radius	< 0.1 pc ~ 10 <sup>5</sup> R <sub>s</sub>	10 <sup>-5</sup>	10 <sup>-5</sup>
Inner accretion	1-10 <sup>3</sup> R <sub>s</sub>	10 <sup>-9</sup> – 10 <sup>-7</sup>	10 <sup>-1</sup> – 10 <sup>-3</sup>

# Sgr A\* is faint because

• Gas supply (stellar winds) is not large enough

• A tiny fraction of gas supplied reaches the black hole!

• The accretion flow is inefficient at radiating away its gravitational binding energy

- If  $T_e \ll T_p$  in RIAF, may not see it ( $P_S \sim \gamma^2$ )
- Alternative: jet? (Falcke & Markoff 2000)



VLBI 7 mm

#### Centaurus A

- Simple jet model (Blandford & Königl 1979)
- Plasma propagates at a constant proper speed ⇒ v<sub>z</sub>=γ<sub>j</sub>β<sub>j</sub>c.
   The (isothermal) plasma
- The (isothermal) plasma expands with sound speed
  - $\Rightarrow$  V<sub>r</sub>= $\gamma_s\beta_s$ C.
- The resulting shape is a cone with Mach number

$$M = \frac{\gamma_{j}\beta_{j}}{\gamma_{s}\beta_{s}} \approx \gamma_{j}\sqrt{c}$$



Taken from http://slideplayer.com/slide/5083341/

- Again hydro conservation laws
- Particle conservation:  $\dot{M}_{j} = \rho \cdot \mathbf{v} \cdot A = m_{p} n(r) \cdot \gamma \beta c \cdot \pi r^{2}$  $\Rightarrow n(r) = \frac{\dot{M}_{j}}{m_{p} \cdot \gamma \beta c \cdot \pi r^{2}} \propto r^{-2}$
- Energy conservation:

$$\dot{E}_{j,mag} = \rho_B \cdot \mathbf{v} \cdot A = \frac{B^2(r)}{8\pi} \cdot \gamma \beta c \cdot \pi P$$
$$\Rightarrow B(r) = \sqrt{\frac{8L_{j,B}}{\gamma \beta c \cdot r^2}} \propto r^{-1}$$



Taken from http://slideplayer.com/slide/5083341/

- If T<sub>e</sub> << T<sub>p</sub> in RIAF, may not see it at all!
- Alternative: jet? (Falcke & Markoff 2000)



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# Infrared/X-ray flares from Sgr A\*

• Sgr A\*: rapidly variable IR/X-ray emission (Baganoff+2001, Genzel+2003, Ghez+2004)



#### Flares must be particle heating



# Electron heating near black holes

 Shock acceleration (jet? tilted disk?) or magnetic reconnection (corona?)



# Flares originate close to the black hole

- Assume:
  - flare is powered by accretion
  - RIAF: B(r)  $\sim$  100G r<sub>g</sub> / R ( $\sim$ same as jet!)
- Observed flare:
  - Region size < c  $\Delta t$ <  $3x10^{12}$  cm (~5r<sub>g</sub>) - L<sub>x</sub> ~ 2x10<sup>35</sup> erg / s, t = 1838 s



#### Flares originate close to the black hole

• E<sub>total</sub> > E<sub>flare</sub>:

 $U_B V > L_X t$ RIAF: B(r) ~ 100 G r<sub>g</sub> / R (~same as jet!)

#### Flares originate close to the black hole

- $E_{total} > E_{flare}$ :  $U_B V > L_X t$ RIAF: B(r) ~ 100 G r<sub>g</sub> / R (~same as jet!)
- $B_0^2 (rg/R)^2 / 8\pi 4 / 3\pi R^3$ >  $L_X t$  $rg < 10 (B_0 / 100G)$



#### Synchrotron spectra

Rybicki & Lightman 1979

•  $P_s = 4/3 \sigma_T c \gamma^2 U_B sin^2 \theta$ 

• Critical frequency  $v_c = 3/4\pi \Omega_B \gamma^2 \sin\theta$ 

•  $dP_s/dv \sim P_s / v_c \sim e^3/mc^2 B \sin\theta F(v/v_c)$ 



#### Synchrotron spectra

Rybicki & Lightman 1979

• Power law particle dist.

$$\begin{split} \mathsf{n}(\mathsf{Y}) &\sim \gamma^{-\mathsf{p}} \\ \mathbf{P}_{\mathrm{tot}}(\nu) &= \int \mathbf{d}\gamma \mathbf{n}(\gamma) \frac{\mathbf{d}\mathbf{P}_{\mathbf{S}}}{\mathbf{d}\nu} \\ \mathbf{P}_{\mathrm{tot}}(\nu) &\propto \int \mathbf{d}\gamma \ \gamma^{-\mathbf{p}} \ \mathbf{F}(\nu/\nu_{\mathbf{c}}) \\ \mathsf{let} \ \mathbf{x} &= \mathsf{v}/\mathsf{v}_{\mathsf{c}'} \ \mathbf{x} \sim \gamma^{-2} \\ \mathbf{P}_{\mathrm{tot}}(\nu) &\propto \nu^{-(\mathbf{p}-1)/2} \int \mathbf{d}\mathbf{x} \ \mathbf{x}^{-(\mathbf{p}-3)/2} \ \mathbf{F}(\mathbf{x}) \end{split}$$

# IR flares are synchrotron radiation

Eckart+2006, 2008



#### X-ray flare radiation mechanisms



v [Hz]

# Particle heating and cooling

- Why would synchrotron X-rays have a break?
- Synchrotron radiation:

 $-n(Y) \sim Y^{-p}, P_{v} \sim v^{-(p-1)/2}$ 

# Particle heating and cooling

- Why would synchrotron X-rays have a break?
- Synchrotron radiation:
  - $-n(Y) \sim Y^{-p}, P_{v} \sim v^{-(p-1)/2}$
  - Electron energy evolution (Blumenthal & Gould 1970):

$$\begin{split} \frac{\partial \mathbf{n}(\boldsymbol{\gamma},\mathbf{t})}{\partial \mathbf{t}} &= \mathbf{Q} - \frac{\partial(\dot{\boldsymbol{\gamma}}\mathbf{n})}{\partial\boldsymbol{\gamma}} - \frac{\mathbf{n}}{\mathbf{t}_{\mathrm{esc}}}\\ & \text{heating cooling escape} \\ \text{Cooling:} \quad \dot{\boldsymbol{\gamma}} &= -\boldsymbol{\gamma}/\mathbf{t}_{\mathrm{cool}} \sim -\boldsymbol{\gamma}^{\mathbf{2}} \\ \mathbf{t}_{\mathrm{cool}} \sim \boldsymbol{\gamma}^{-1}\mathbf{B}^{-\mathbf{2}} & \text{Cooling fast at X-rays,}\\ & \text{`slow in IR!} \end{split}$$
# Particle acceleration and cooling

 $\begin{array}{l} - \text{ Electron energy evolution} \\ \text{(Blumenthal & Gould 1970):} \\ \frac{\partial \mathbf{n}(\gamma, \mathbf{t})}{\partial \mathbf{t}} = \mathbf{Q} - \frac{\partial (\dot{\gamma} \mathbf{n})}{\partial \gamma} - \frac{\mathbf{n}}{\mathbf{t}_{\mathrm{esc}}} \end{array}$ 

Steady state, no cooling:  $n(\gamma) = Q t_{esc}$ 

Particles heat until they escape;
input e- spectrum → output IR spectrum with
s = (p-1)/2

### Particle acceleration and cooling

 $\begin{array}{l} - \text{ Electron energy evolution} \\ \text{(Blumenthal & Gould 1970):} \\ \frac{\partial \mathbf{n}(\gamma, \mathbf{t})}{\partial \mathbf{t}} = \mathbf{Q} - \frac{\partial (\dot{\gamma} \mathbf{n})}{\partial \gamma} - \frac{\mathbf{n}}{\mathbf{t}_{\mathrm{esc}}} \end{array}$ 

Steady state, rapid cooling:

look for solution n ~  $\gamma^{-s}$  with Q ~  $\gamma^{-p}$ :

$$\mathbf{Q}\sim rac{\dot{\gamma}\mathbf{n}}{\gamma}$$
 or  $\mathbf{n}(\gamma)\sim \mathbf{Q}/\gamma$ 

 $\rightarrow$  "Cooling break" in spectrum between IR, X-rays

### Evidence for synchrotron X-rays



# Evidence for synchrotron flares

Dodds-Eden+2009

• For inverse Compton:

$$\gamma^{2} < v_{X-ray} / v_{NIR} < 1000$$

$$v_{\rm C} = 4.2 \times 10^6 \, \text{B} \, \gamma^2 > v_{\rm NIR} \rightarrow \text{B} > 25 \, \text{G}$$

$$P_{S} / P_{C} = U_{B} / U_{ph} \sim 1$$

Synchrotron size < 0.1 r<sub>g</sub> tiny!

→ Unrealistic emission region sizes (and/or other parameters) for Compton scenarios

#### Simultaneous IR/X-ray spectra



Even stronger evidence!



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